# Model a cylindrical cavity with the CST Microwave Studio

## Evgenya I. Simakov

## Los Alamos National Laboratory

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## Model set up for the $\pi$ -mode

- Draw a cylindrical cavity with iris.
  - Length:  $\lambda/2$  ( $\pi$ -mode)
  - Thickness of the iris: 2 mm
  - Three iris radii: 0.05\*λ, 0.1\*λ, 0.2\*λ
- Tune to 11.424 GHz:
  - Radius: optimize numerically







## Model set up for the $2\pi/3$ -mode

- Draw a cylindrical cavity with iris.
  - Length: λ/3 (2π/3-mode)
  - Thickness of the iris: 2 mm
  - Iris radius 0.1\*λ
- Define periodic boundary conditions.
- Tune to 11.424 GHz:
  - Radius: optimize numerically
- Plot the dispersion curve: frequency vs. phase shift per cell (~ 5 points).







## **Compute:**

- Quality factor Q<sub>0</sub>.
- Shunt impedance R<sub>s</sub>.
- Accelerating gradient E<sub>a</sub>.
- Peak surface electric field E<sub>p</sub>.
- Peak surface magnetic field H<sub>p</sub>.
- The ratios of  $E_p/E_a$ ,  $zH_p/E_a$ .





## **Scattering matrix studies**

 Calculate the scattering matrix for the half-cell with the iris radius 0.1\*λ.







Study the 2π/3-mode cavity with iris radii 0.05\*λ and 0.2\*λ. Tune, compute the dispersion curves and the accelerator characteristics.





#### Results for the $\pi$ -mode, a=0.05\* $\lambda$ .

- R0=10.078 mm, L=13.12 mm.
- Quality factor  $Q_0 = 8550$ .
- Shunt impedance R<sub>s</sub>=1.71\*10<sup>6</sup>.
- Voltage V=3.788\*10<sup>6</sup>. Accelerating gradient E<sub>a</sub>= 288 MV/m.
- Peak surface electric field  $E_p = 570 \text{ MV/m}$ .
- Peak surface magnetic field  $H_p = 753$  kA/m.
- E<sub>p</sub>/ E<sub>a</sub>=1.97; Z\*H<sub>p</sub>/ E<sub>a</sub>=0.98.





#### Results for the $\pi$ -mode, a=0.1\* $\lambda$ .

- R0=10.167 mm, L=13.12 mm.
- Quality factor  $Q_0 = 8609$ .
- Shunt impedance R<sub>s</sub>=1.61\*10<sup>6</sup>.
- Voltage V=3.660\*10<sup>6</sup>. Accelerating gradient E<sub>a</sub>= 279 MV/m.
- Peak surface electric field  $E_p = 548 \text{ MV/m}$ .
- Peak surface magnetic field H<sub>p</sub> = 748 kA/m.
- E<sub>p</sub>/ E<sub>a</sub>=1.96; Z\*H<sub>p</sub>/ E<sub>a</sub>=1.01.





#### Results for the $\pi$ -mode, a=0.2\* $\lambda$ .

- R0=10.394 mm, L=13.12 mm.
- Quality factor  $Q_0 = 8919$ .
- Shunt impedance R<sub>s</sub>=1.64\*10<sup>6</sup>.
- Voltage V=3.630\*10<sup>6</sup>. Accelerating gradient E<sub>a</sub>= 277 MV/m.
- Peak surface electric field  $E_p = 410 \text{ MV/m}$ .
- Peak surface magnetic field H<sub>p</sub> = 720 kA/m.
- E<sub>p</sub>/ E<sub>a</sub>=1.48; Z\*H<sub>p</sub>/ E<sub>a</sub>=0.98.





#### Results for the $2\pi/3$ -mode, $a=0.05*\lambda$ .

- R0=10.101 mm, L=8.75 mm.
- Quality factor  $Q_0 = 6534$ .
- Shunt impedance R<sub>s</sub>=1.04\*10<sup>6</sup>.
- Voltage V=3.381\*10<sup>6</sup>. Accelerating gradient E<sub>a</sub>= 387 MV/m.
- Peak surface electric field  $E_p = 730 \text{ MV/m}$ .
- Peak surface magnetic field  $H_p = 967 \text{ kA/m}$ .
- E<sub>p</sub>/ E<sub>a</sub>=1.89; Z\*H<sub>p</sub>/ E<sub>a</sub>=0.94.





## Dispersion for the $2\pi/3$ -cavity, $a=0.05^*\lambda$ .







#### Results for the $2\pi/3$ -mode, $a=0.1^*\lambda$ .

- R0=10.299 mm, L=8.75 mm.
- Quality factor  $Q_0 = 6563$ .
- Shunt impedance R<sub>s</sub>=0.657\*10<sup>6</sup>.
- Voltage V=2.681\*10<sup>6</sup>. Accelerating gradient E<sub>a</sub>= 306 MV/m.
- Peak surface electric field  $E_p = 718 \text{ MV/m}$ .
- Peak surface magnetic field H<sub>p</sub> = 958 kA/m.
- E<sub>p</sub>/ E<sub>a</sub>=2.34; Z\*H<sub>p</sub>/ E<sub>a</sub>=1.18.





## Dispersion for the $2\pi/3$ -cavity, $a=0.1*\lambda$ .







#### Results for the $2\pi/3$ -mode, $a=0.2^*\lambda$ .

- R0=11.289 mm, L=8.75 mm.
- Quality factor  $Q_0 = 6767$ .
- Shunt impedance R<sub>s</sub>=2.23\*10<sup>5</sup>.
- Voltage V=1.539\*10<sup>6</sup>. Accelerating gradient E<sub>a</sub>= 176 MV/m.
- Peak surface electric field  $E_p = 669 \text{ MV/m}$ .
- Peak surface magnetic field  $H_p = 907$  kA/m.





## Dispersion for the $2\pi/3$ -cavity, $a=0.2^*\lambda$ .





