

# Fundamentals of Accelerators

## Lecture 1

# Motivations & policy

William A. Barletta

Director, United States Particle Accelerator School

Dept. of Physics, MIT

Faculty of Economics, University of Ljubljana



# Energy & Momentum units

- ❖ When we talk about the energy or momentum of individual particles, the Joule is inconvenient
- ❖ Instead we use the eV, the energy that a unit charge

$$e = 1.6 \times 10^{-19} \text{ Coulomb}$$

gains when it falls through a potential,  $\Delta\Phi = 1$  volt.

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ Joule}$$

- ❖ For momentum we use the unit, eV/c, where c is the speed of light



# Mass units

- ❖ We can use Einstein's relation,

$$E_o = mc^2$$

to convert rest mass to energy units (m is the rest mass)

- ❖ For electrons,

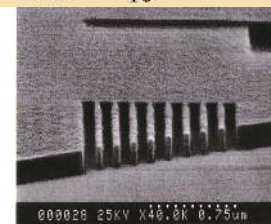
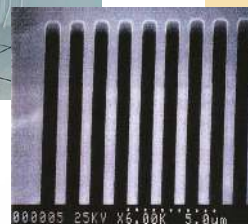
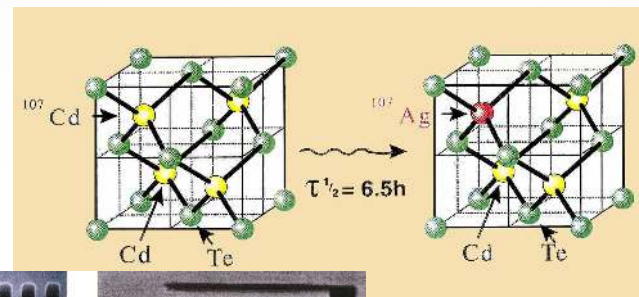
$$\begin{aligned} E_{o,e} &= 9.1 \times 10^{-31} \text{ kg} \times (3 \times 10^8 \text{ m/sec})^2 = 81.9 \times 10^{-15} \text{ J} \\ &= 0.512 \text{ MeV} \end{aligned}$$

- ❖ For protons,

$$E_{o,p} = 938 \text{ MeV}$$



# Accelerators are the hallmark of highly technological societies

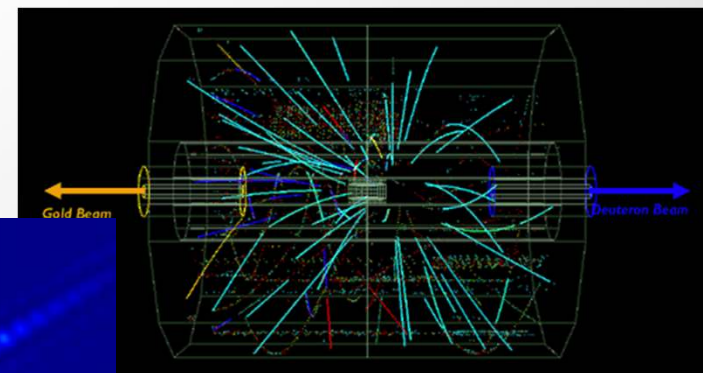
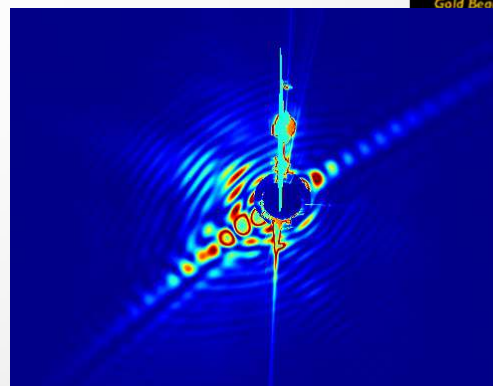


*Materials*

*Medicine*



*Basic Research*



Brookhaven National Lab / RHIC-STAP Collaboration

*Exciting products...  
exciting opportunities*

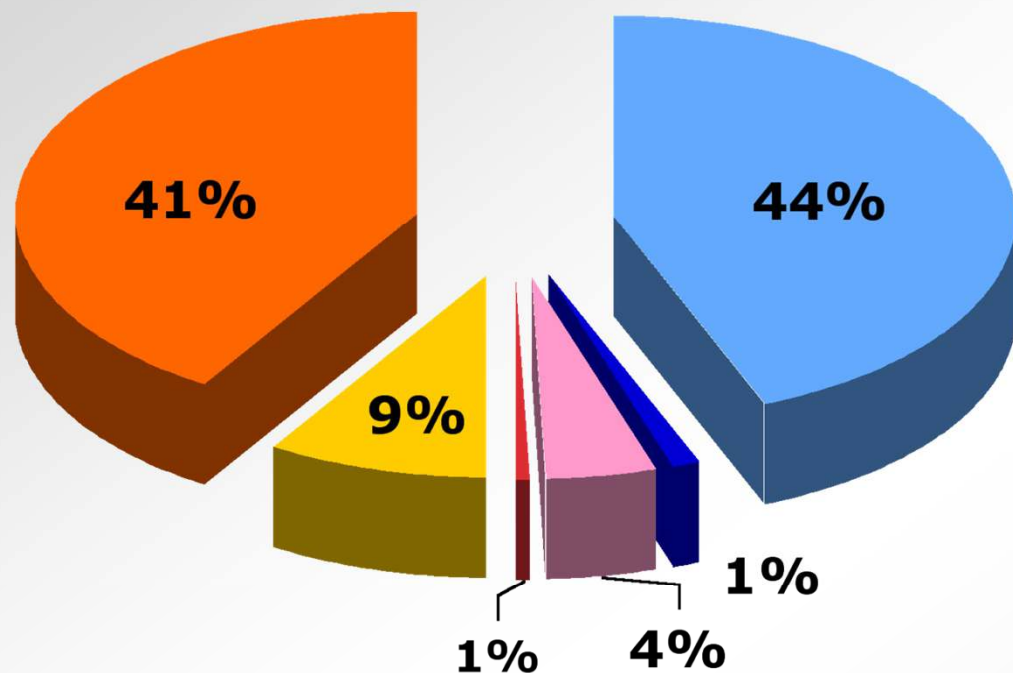




# Accelerators are big business

## Academic researchers are “the 1%”

**Number of accelerators worldwide**  
**~ 26,000**



- Radiotherapy (>100.000 treatments/yr)\*
- Medical Radioisotopes
- Research (incl. biomedical)
- >1 GeV for research
- Industrial Processing and Research
- Ion Implanters & Surface Modification

*Annual growth is several percent*

**Sales >3.5 B\$/yr**

**Value of treated good > 50 B\$/yr \*\***

*Major research machines are a tiny fraction of the total, but...*



# Research: How can we understand the underlying structure of things?

The first “light source”



*Wilhelm Röntgen discovered X-rays in 1895  
by accelerating electrons*



# Motivations: How it all began

## Paradigm 1: Fixed target experiments

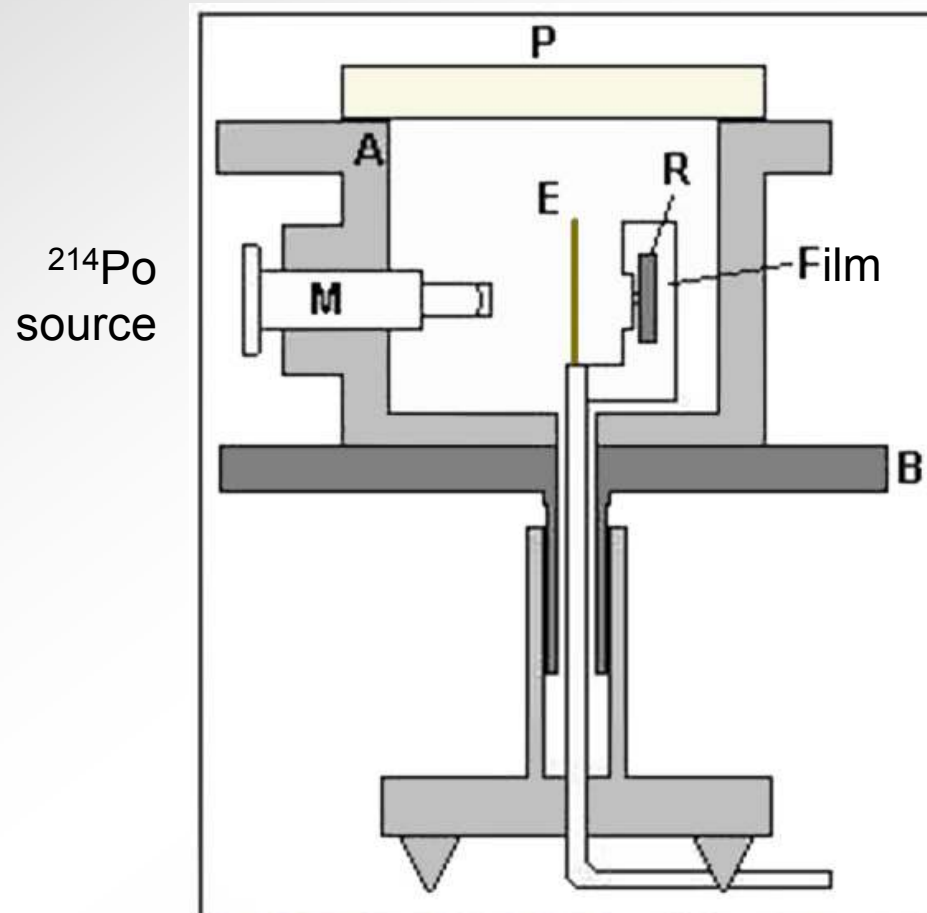


Fig1. Marsden-Geiger experiment.

Rutherford explains scattering of *alpha particles* on gold discovering the nucleus & urges ... *On to higher energy probes!*

# Rutherford articulated Figure of Merit 1

*Particle (or photon) energy on target*



# Why we use energetic beams for research?

## ❖ Resolution of "Matter" Microscopes

- Wavelength of Particles ( $\gamma$ , e, p, ...) (de Broglie, 1923)

$$\lambda = h / p = 1.2 \text{ fm} / p [\text{ GeV}/c]$$

- Higher momentum  $\Rightarrow$  shorter wavelength  $\Rightarrow$  better resolution

## ❖ Energy to Matter

- Higher energy produces heavier particles



# The advantage of the fixed target physics: Figure of Merit 2

$$\frac{\text{Events}}{\text{second}} = \sigma_{\text{process}} \underbrace{\square \text{Flux} \square \text{Target Number Density} \square \text{Path Length}}_{\text{Luminosity}}$$

*Typical values:*

$$\text{Flux} \sim 10^{12} - 10^{14} \text{ s}^{-1}$$

$$\text{Number density} \sim \rho N_A Z/A \sim 5 \times 6 \times 10^{23} / 2$$

$$\text{Path length} \sim 10 \text{ cm}$$

$$\text{Luminosity} \sim 15 \times 10^{23} \times 10^{14} \sim 10^{36} - 10^{38} \text{ cm}^{-2} \text{ s}^{-1}$$

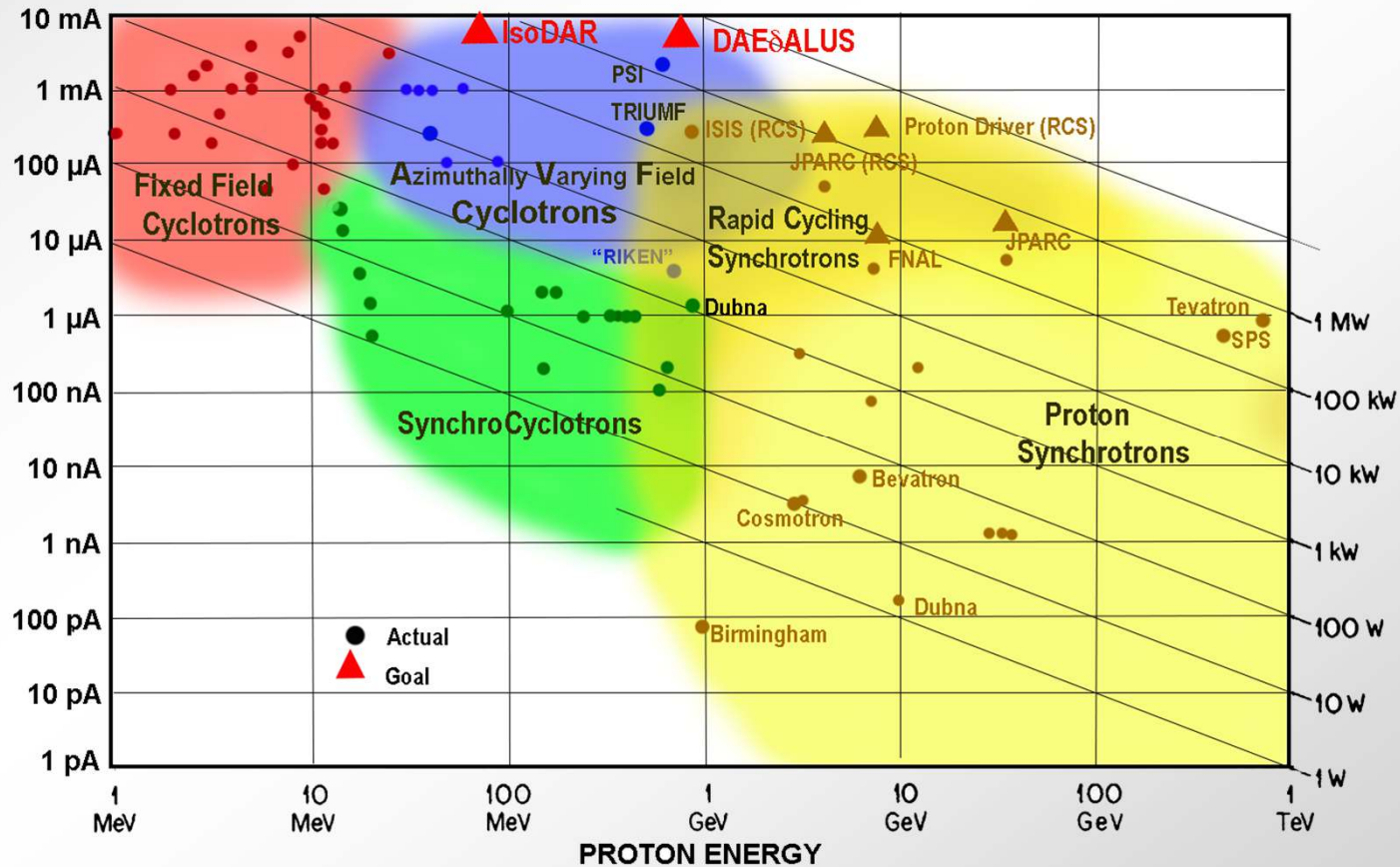
*Ideal for precision & rare process physics,  
BUT how much energy is available for new physics*





# Fixed targets require high power beams

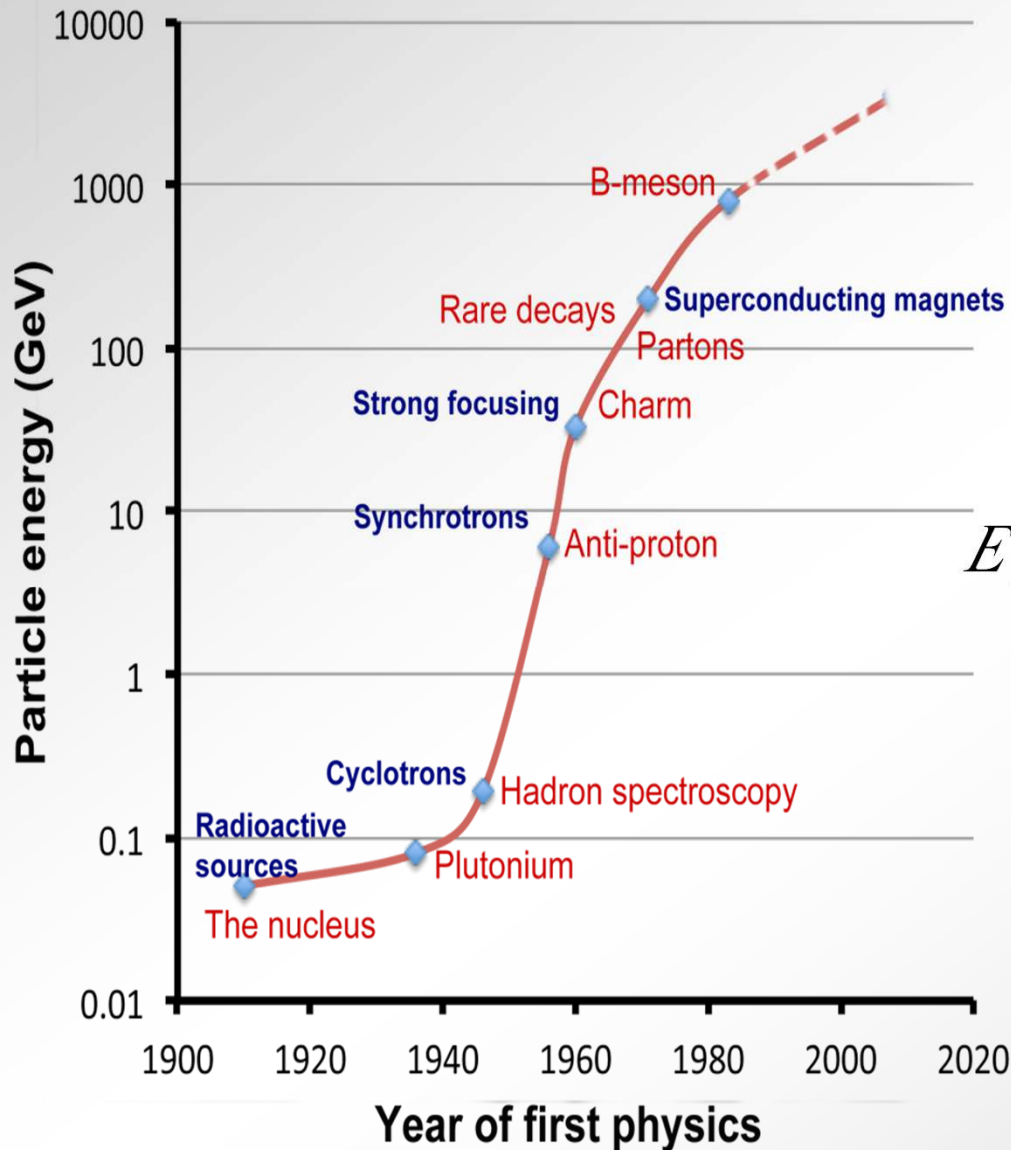
- ❖ For current  $< 5$  mA, circular accelerators are economical
  - Current limit  $\sim 5$  mA (space charge at injection)  $<$  Linac
  - Energy limit  $\sim 1$  GeV  $\ll$  Linac potential
  - \$\$ per MW  $\sim 1/4$  of Linac of same beam parameters







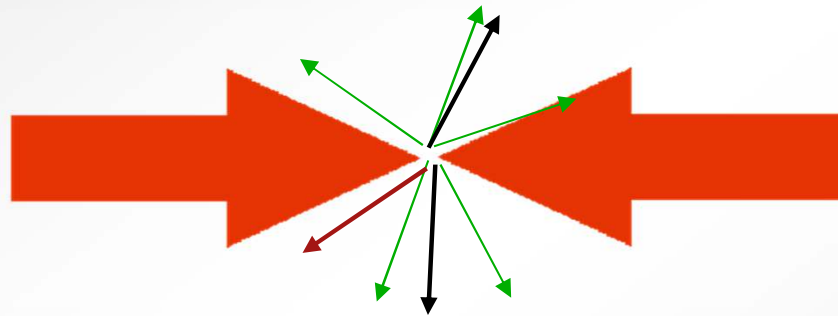
# The fixed target paradigm has its limits



Invariance of  
 $(p_1 + p_2)^\mu \cdot (p_1 + p_2)_\mu$   
in Lorentz frames implies that

$$E_{cm} = \sqrt{m_1^2 + m_2^2 + 2m_2 c^2 E_{beam}}$$
$$\approx \sqrt{2mc^2 E_{beam}} \text{ for equal masses}$$

## Collide beams !



If  $m_1 = m_2$  and if  $E_1 = E_2 = E$

$$E_{cm} = 2 E$$

*The full kinetic energy of both particles  
is now available to physical processes*



# The next big step was the ISR at CERN

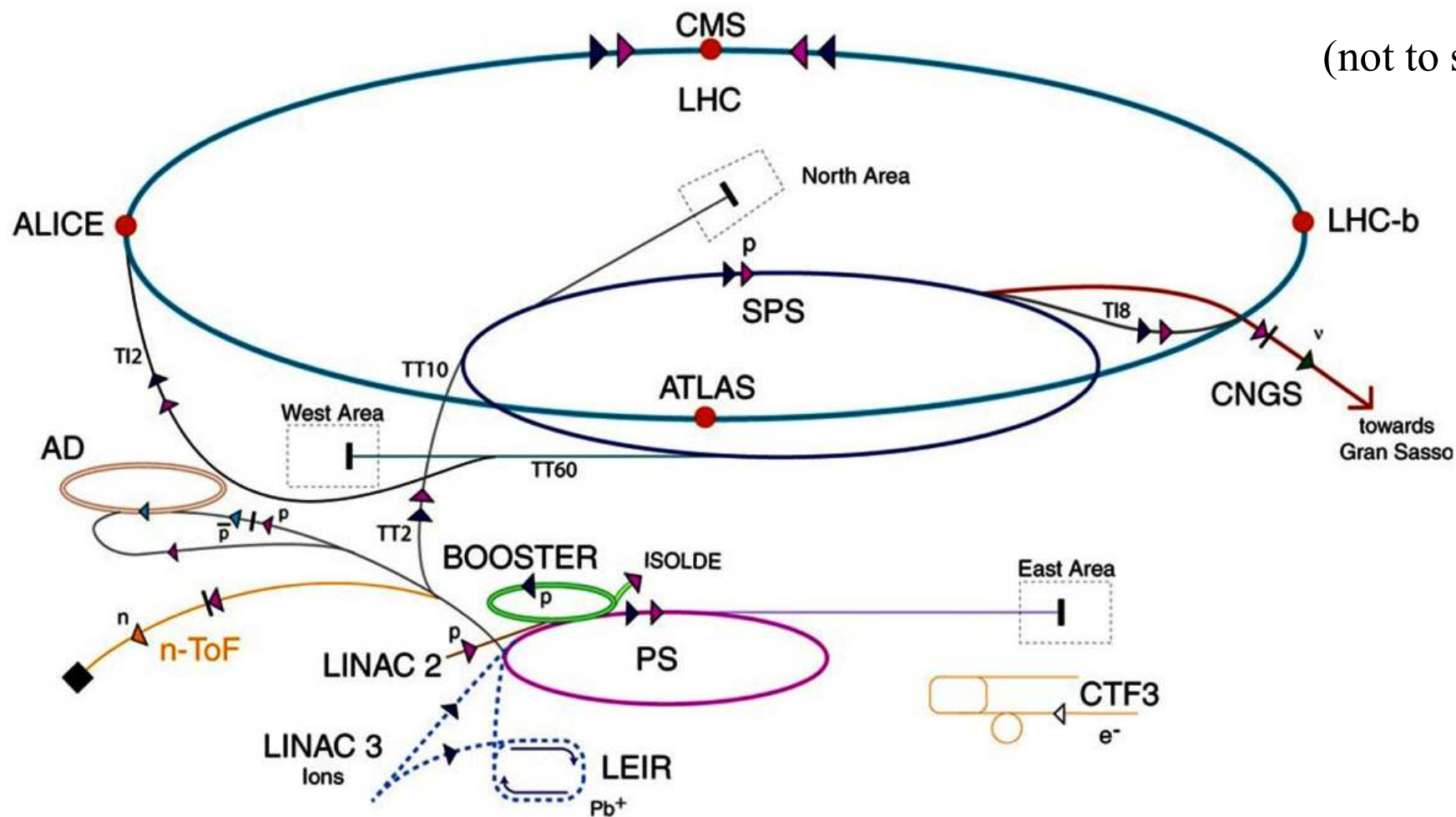
- ❖ 30 GeV per beam with  $> 60$  A circulating current
  - Required extraordinary vacuum ( $10^{-11}$  Torr)
  - Great beam dynamics challenge - more stable than the solar system
- ❖ Then on to the 200 GeV collider at Fermilab (1972) and ...
- ❖ The Sp $\bar{p}$ S at CERN
  - *Nobel invention:*  
Stochastic cooling
- ❖ Then the Tevatron
  - Required a *major technological invention*



First machine to exploit  
superconducting magnet technology



# The largest research accelerator: CERN Accelerator Complex (LHC)



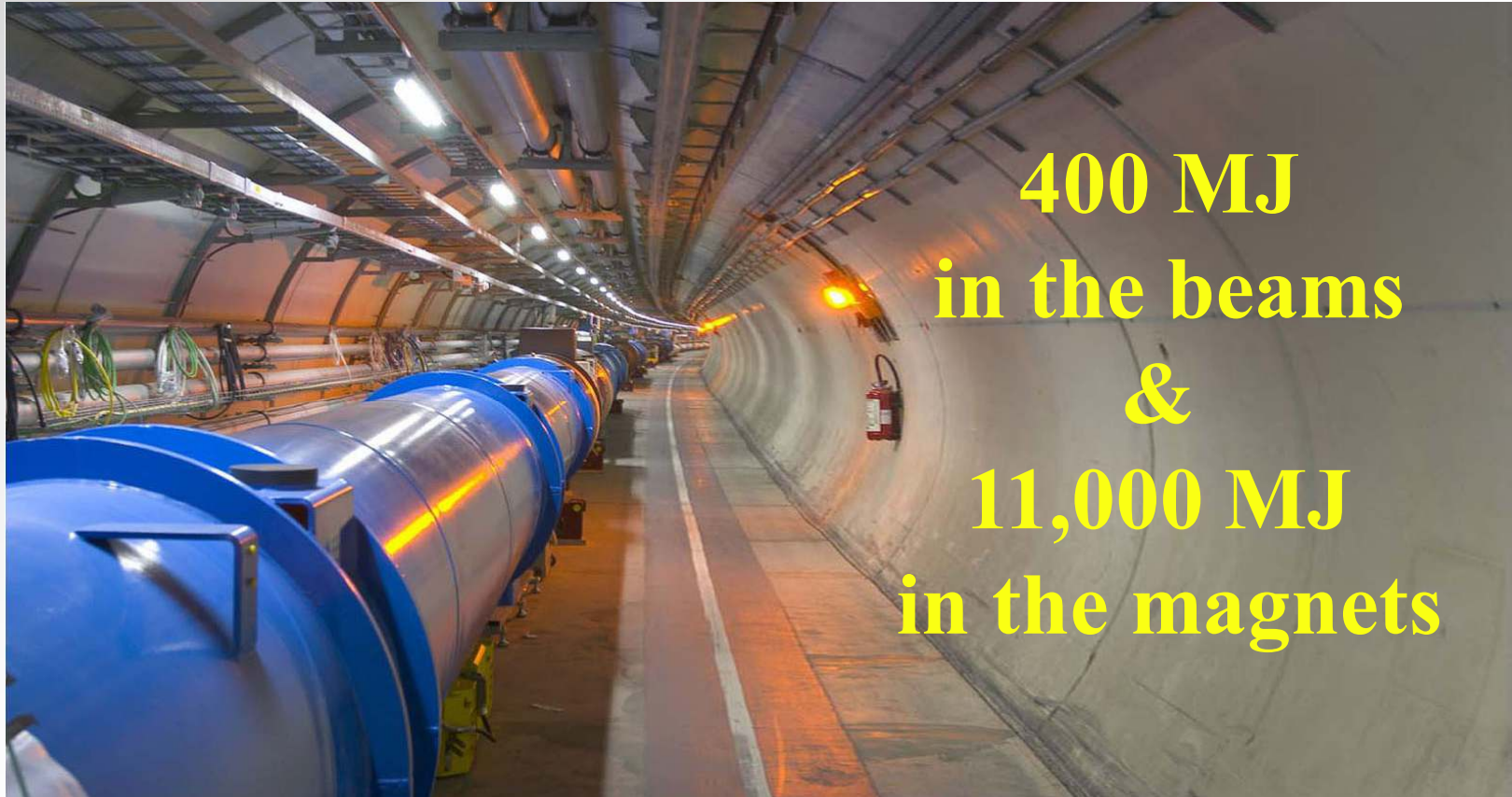
- |            |               |                              |                                |
|------------|---------------|------------------------------|--------------------------------|
| ▶ protons  | ▶ antiprotons | AD Antiproton Decelerator    | LHC Large Hadron Collider      |
| ▶ ions     | ▶ electrons   | PS Proton Synchrotron        | n-ToF Neutron Time of Flight   |
| ▶ neutrons | ▶ neutrinos   | SPS Super Proton Synchrotron | CNGS CERN Neutrinos Gran Sasso |
|            |               |                              | CTF3 CLIC Test Facility 3      |





# The future of HEP runs through CERN

## “Après moi, le déluge”



- LHC upgrades rely on advances in magnet technology
  - Luminosity upgrade - very high gradient, Nb<sub>3</sub>Sn quads
  - Super LHC (energy upgrade) - very high field dipoles



# What sets beam size ?

- ❖ Strength (depth of focus) of lens at interaction point,  $\beta^*$
- ❖ Distribution of positions & transverse momenta of beam particles (emittance),  $\varepsilon$

$$\sigma_{x,y} = \sqrt{\varepsilon_{x,y}^*}$$

$$\text{Luminosity} = \frac{N_1 \times N_2 \times f}{4\pi \sqrt{\varepsilon_x^* \varepsilon_y^*}} \times \text{Pinch effect} \times \text{angle correction}$$

- ❖ For simplicity say  $\varepsilon$  and  $\beta^*$  are equal for x and y

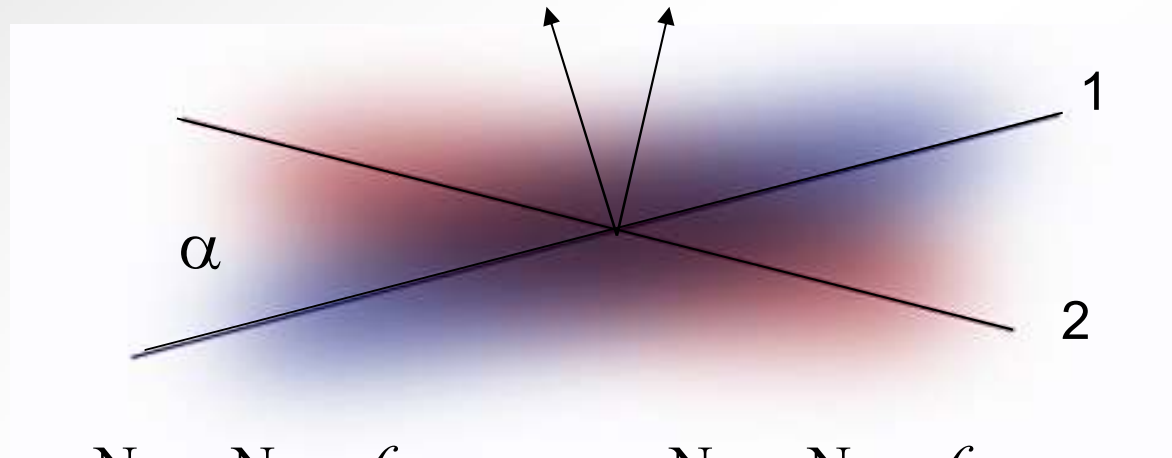
$$\text{Luminosity} = \frac{N_1 \times N_2 \times f}{4\pi \varepsilon_x^*} \times H_D \times \text{angle correction}$$



# This looks too good to be true! What about the luminosity?

$$\text{Events} = \text{Cross-section} \times \langle \text{Collision Rate} \rangle \times \text{Time}$$

*Beam energy: sets scale of physics accessible*



$$\text{Luminosity} = \frac{N_1 \times N_2 \times \text{frequency}}{\text{Overlap Area}} = \frac{N_1 \times N_2 \times f}{4\pi\sigma_x\sigma_y} \times \text{Correction factors}$$

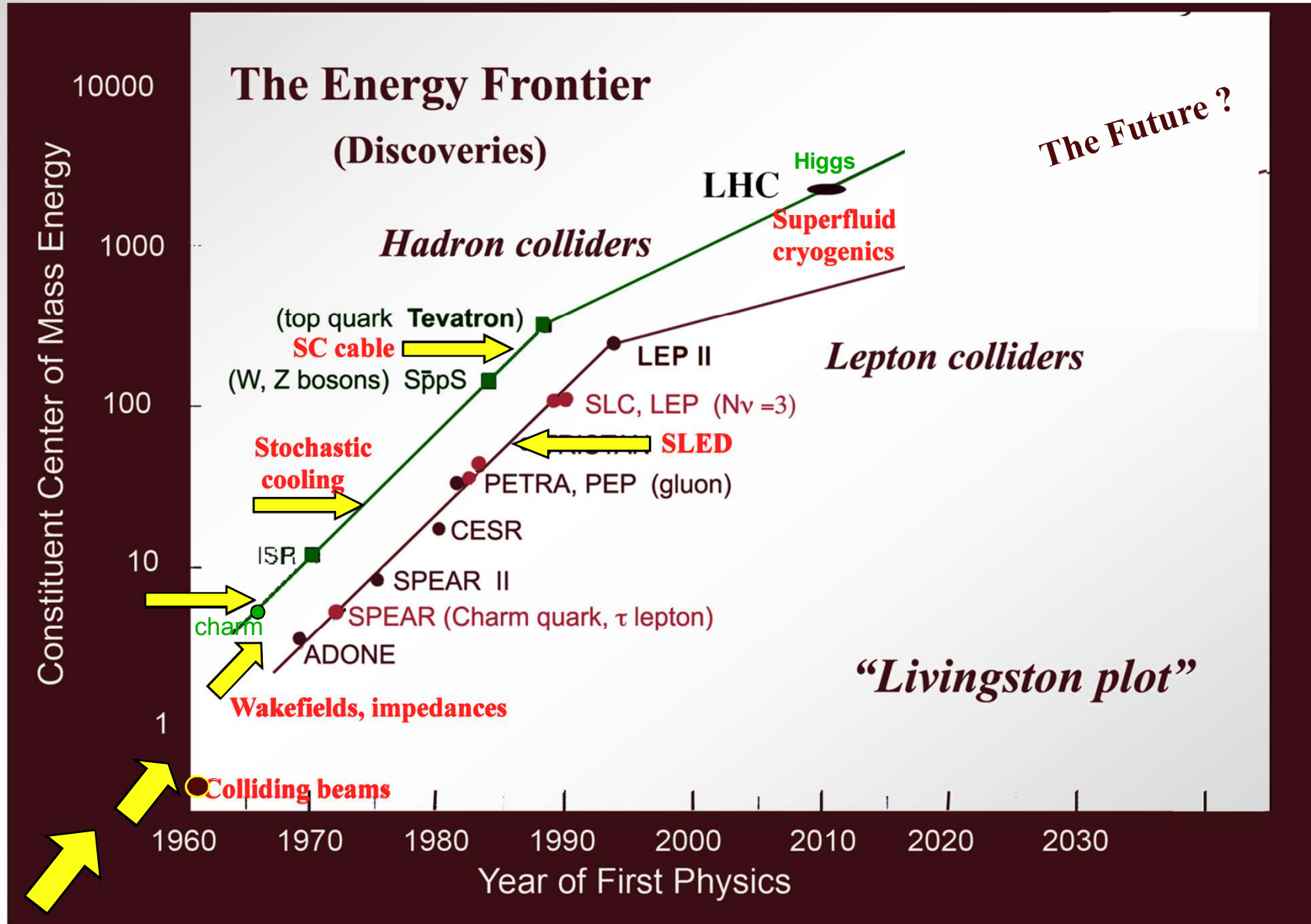
*We want large charge/bunch, high collision frequency & small spot size*

$$\text{Luminosity} \sim 10^{31} - 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$





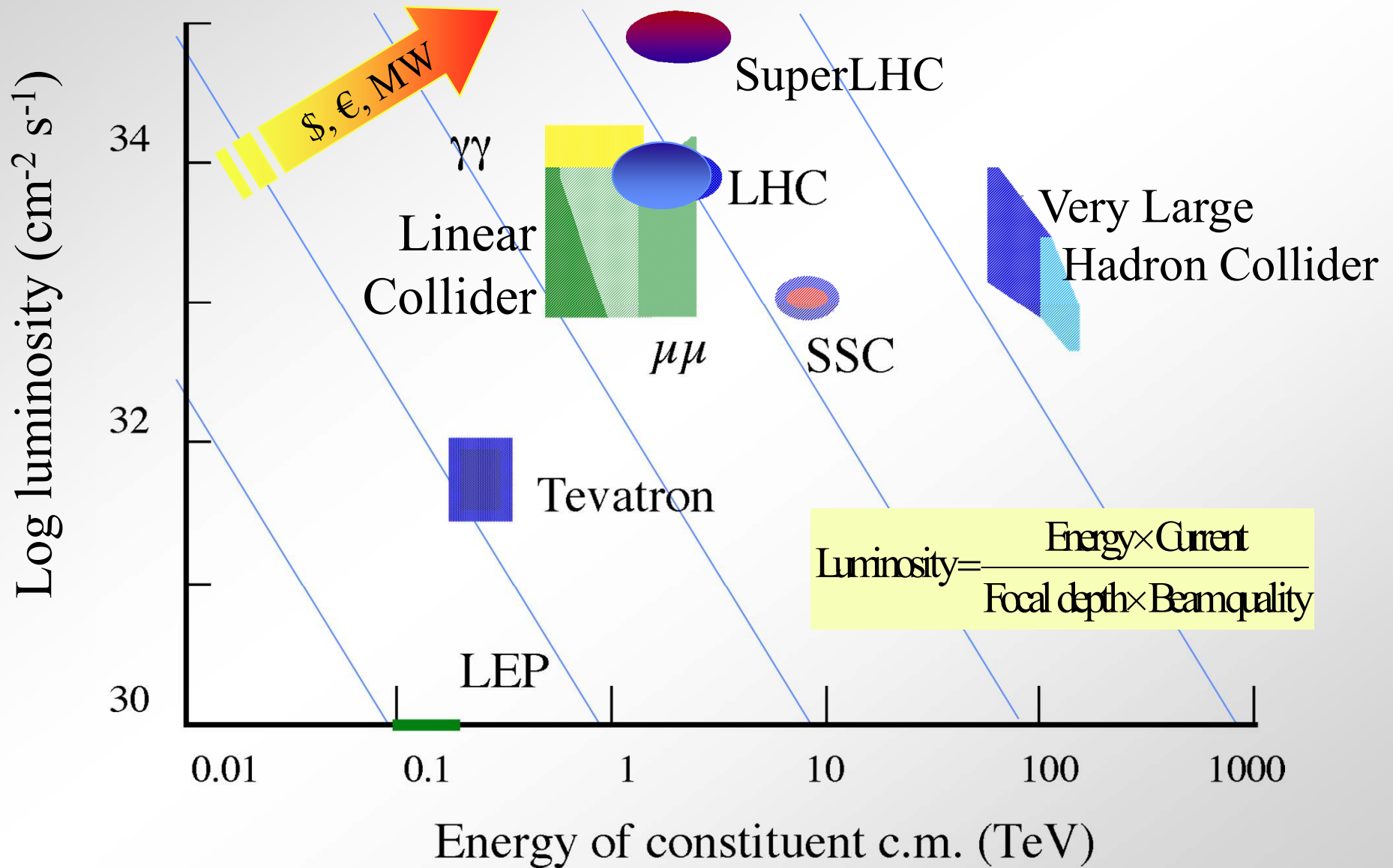
# Energy frontier is extended by inventions in accelerator technology (in red)



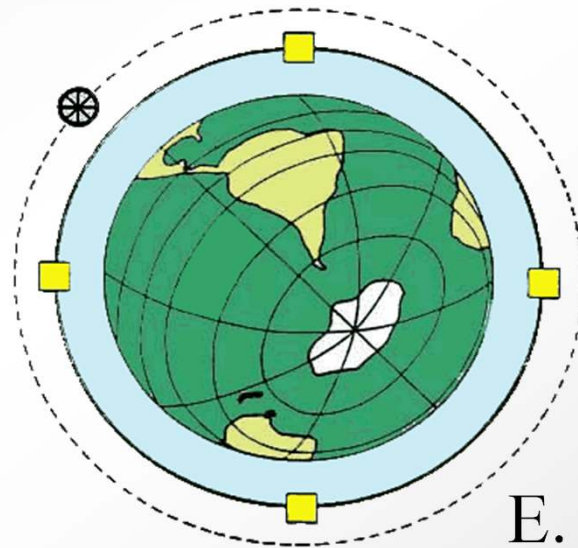
## 10 minute exercise:

Show explicitly that the expression for  
collider luminosity  
is equivalent to the expression for  
fixed target luminosity.

# Example from High Energy Physics: Discovery space for future accelerators

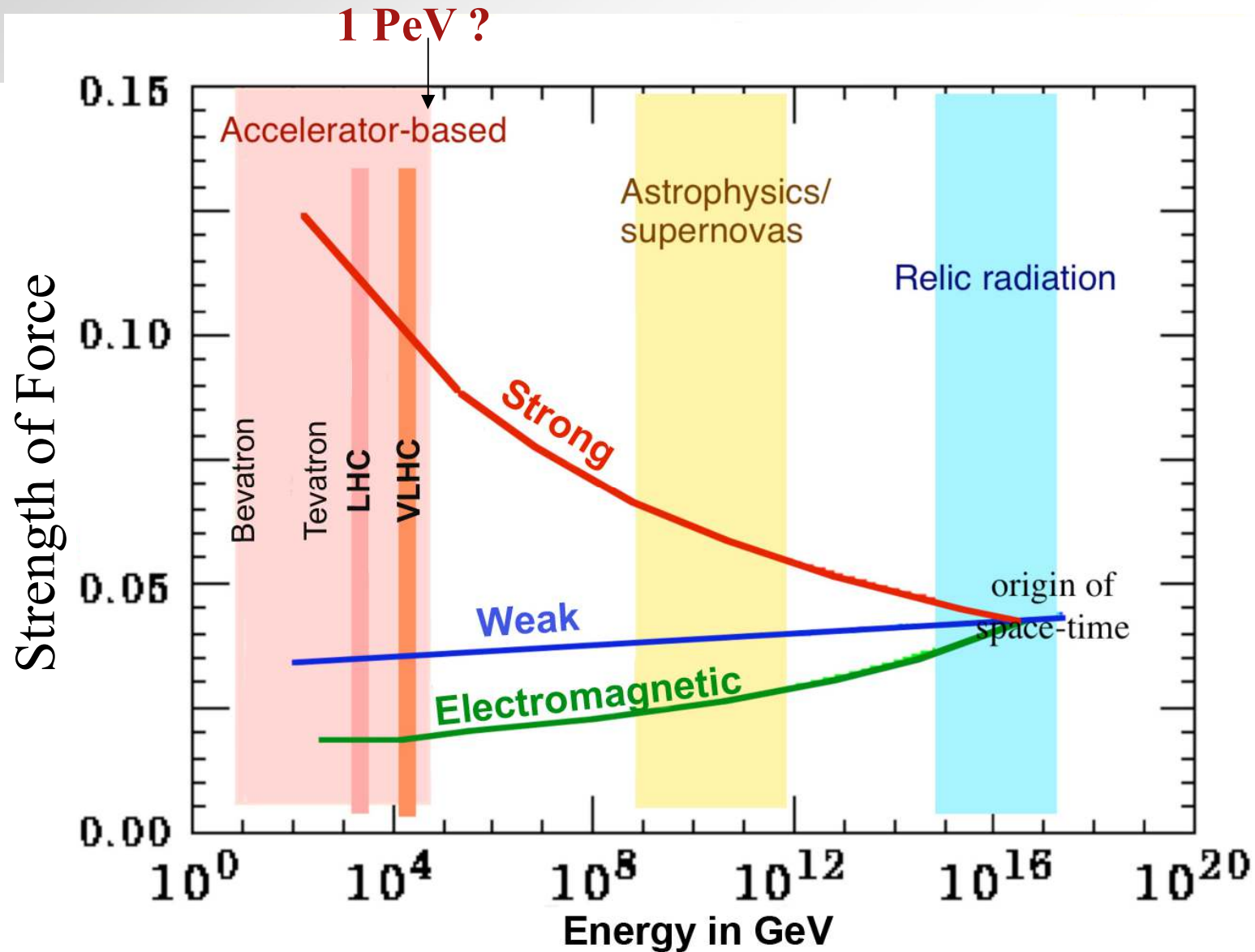


# Limits of accelerator-based HEP



E. Fermi

# How far can we go with this approach?



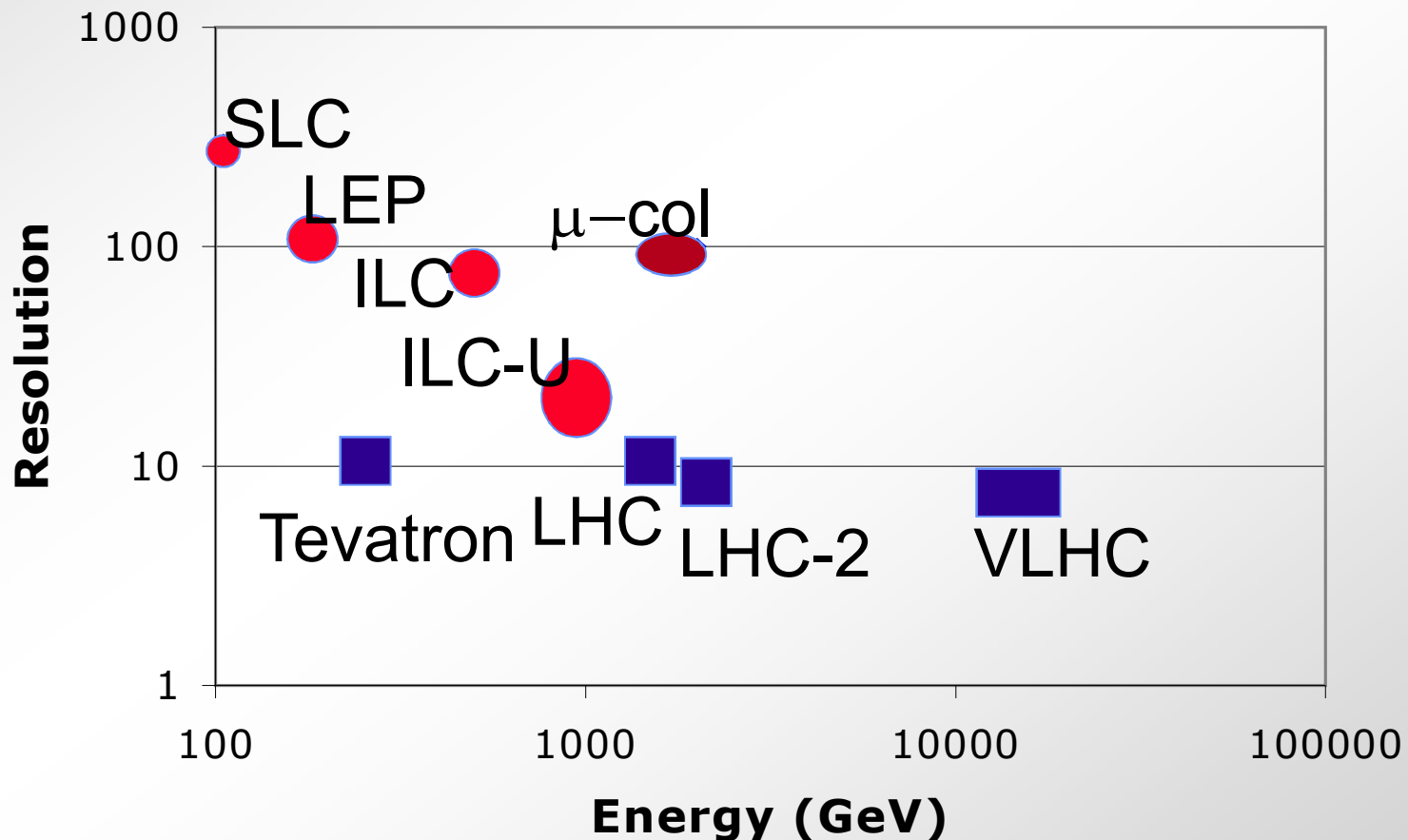


# How big is a PeV collider?



## FoM 3: Resolution (Energy/ $\Delta$ Energy)

- ❖ Intertwined with detector & experiment design
  - In hadron colliders: production change, parton energy distribution
  - In lepton colliders: energy spread of beams (synchrotron radiation)

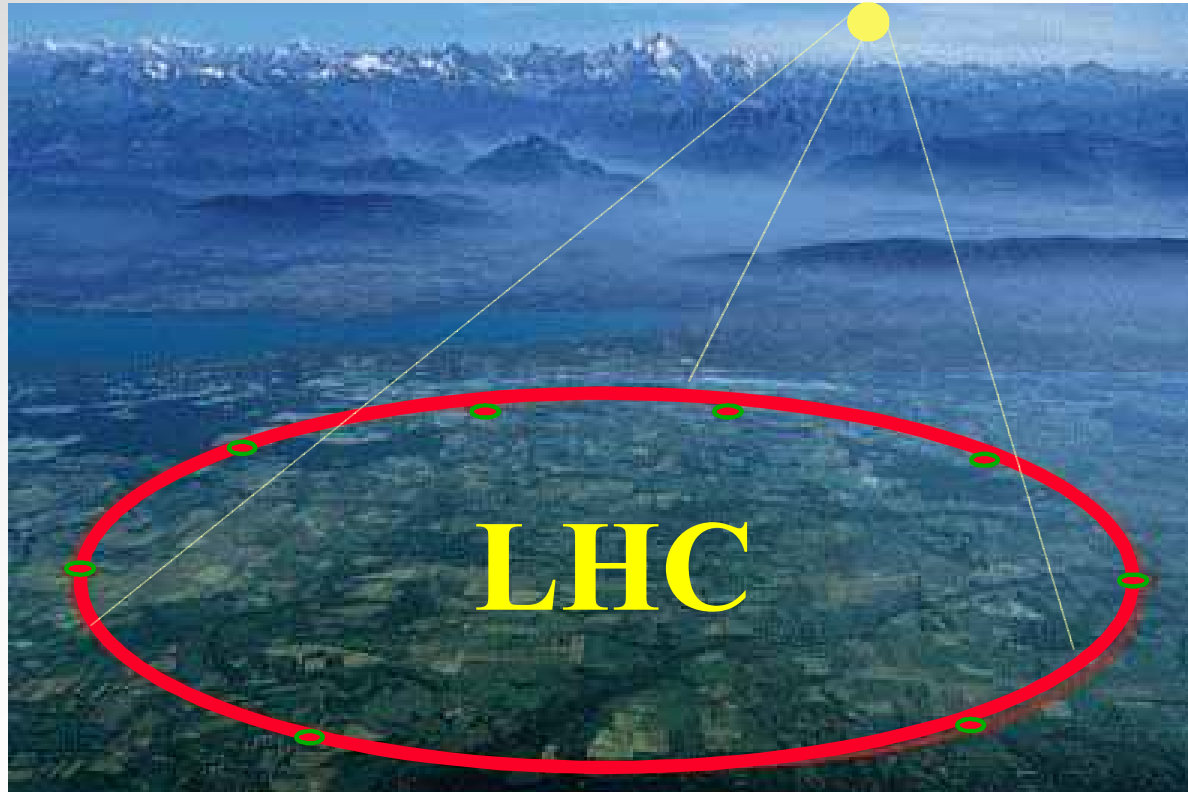






# The future of HEP runs through CERN

## “Après moi, le déluge”

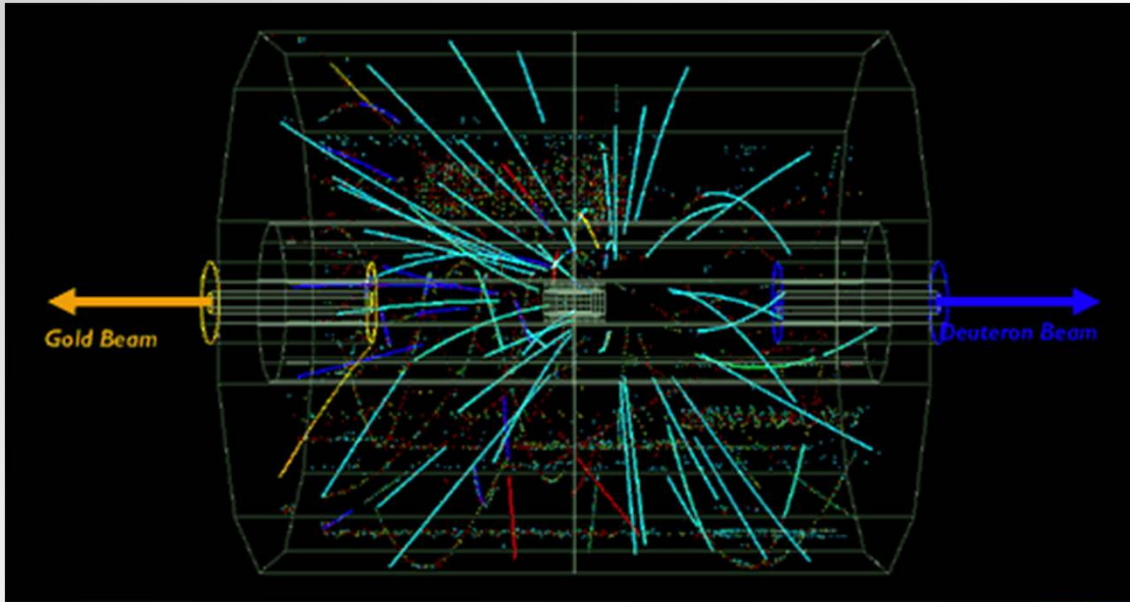


- LHC upgrades rely on advances in magnet technology
  - Reliability upgrade (2013) - replace IR Quads & collimators
  - Luminosity upgrade - very high gradient, Nb<sub>3</sub>Sn quads
  - Super LHC (energy upgrade) - very high field dipoles

# Nuclear Physics



# High energy studies of QCD: Heavy ion collisions using synchrotrons



Brookhaven National Lab / RHIC-STAR Collaboration

## D - Au at RHIC => Nuclear superfluid

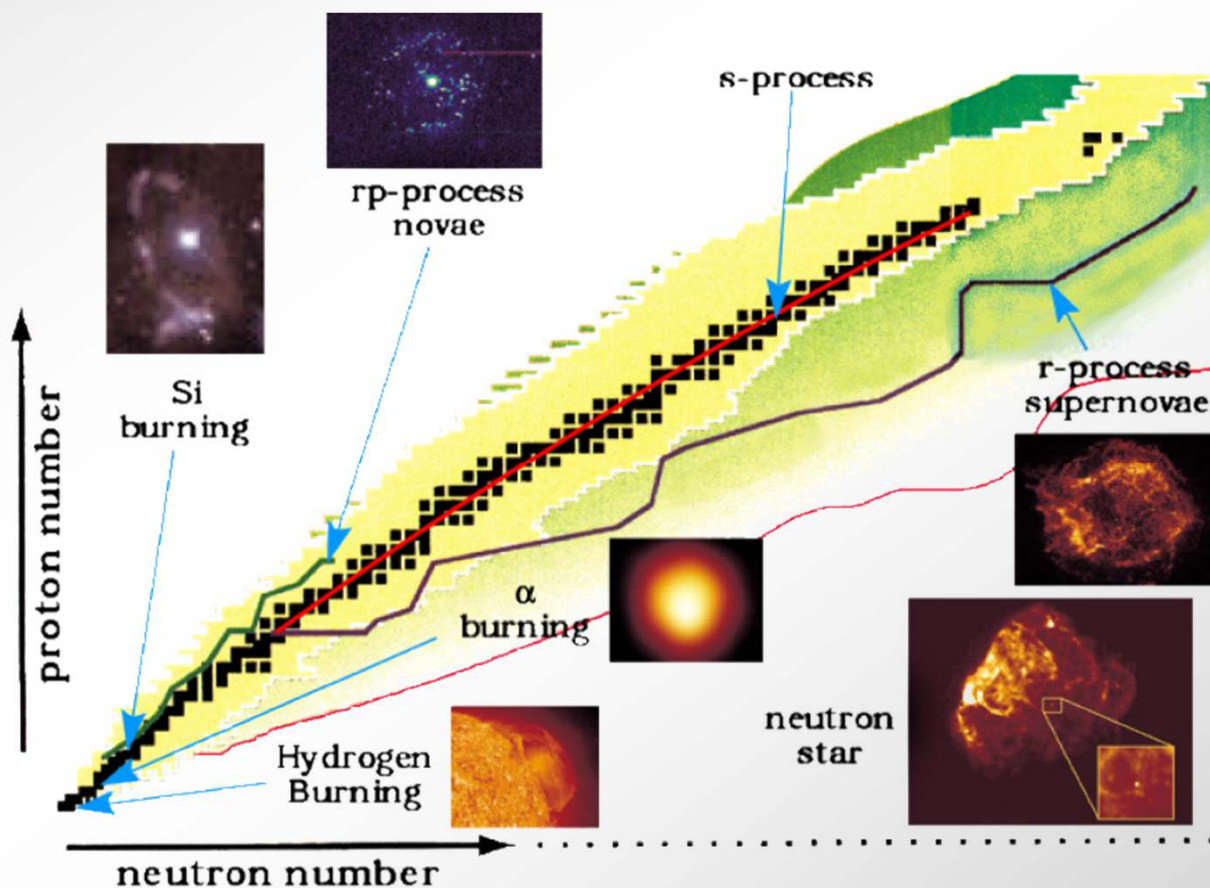
## Next ALICE @ LHC => Quark-gluon plasma





# Nuclear Astrophysics - Nature of Hadronic Matter: Radioactive Beam Facilities

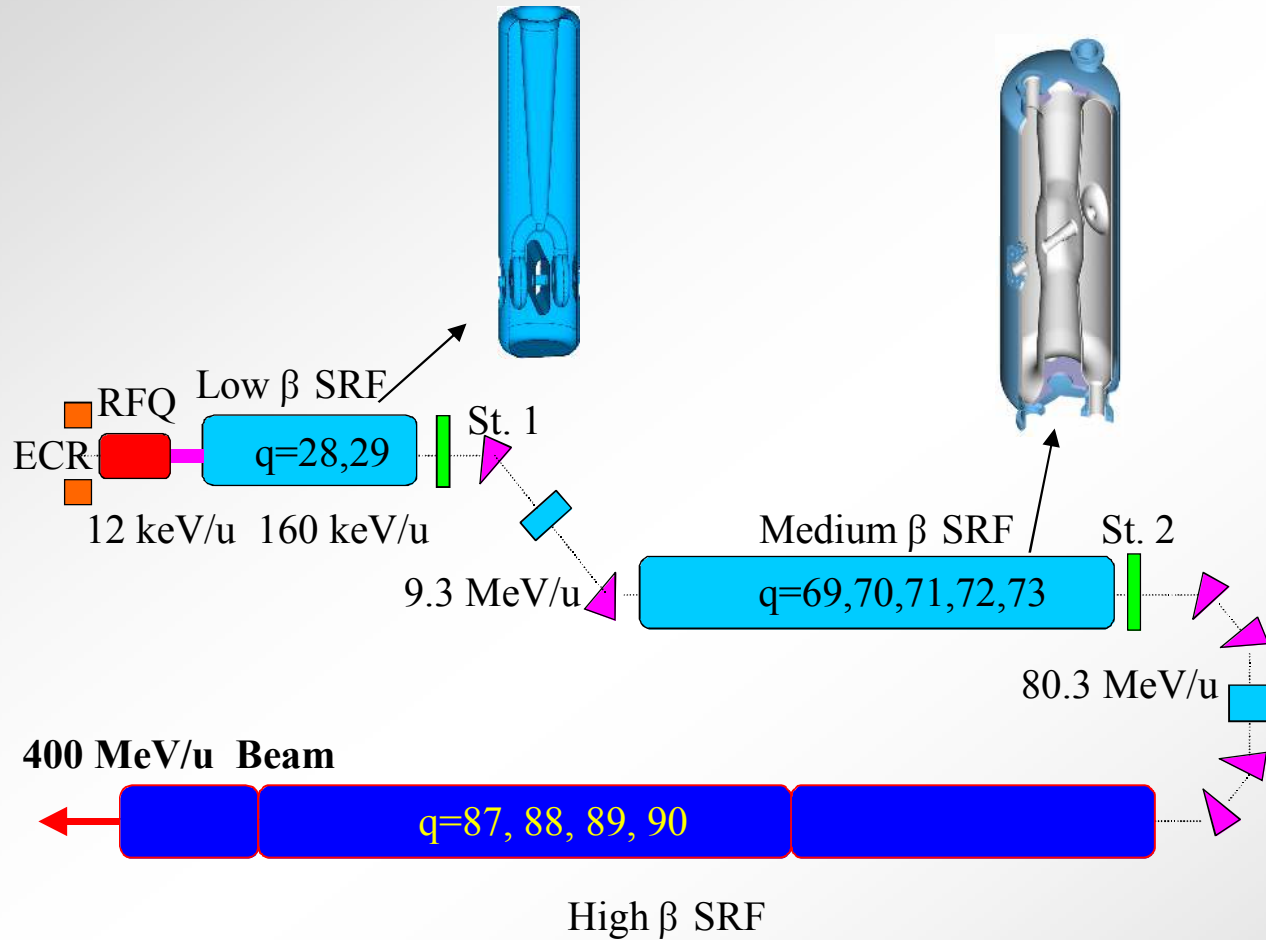
- a Explore nuclear structure & reactions involving nuclei far from the valley of stability
  - U These nuclei participate in explosive nucleo-synthesis in novae, x-ray bursts, and supernovae via rapid proton and neutron capture







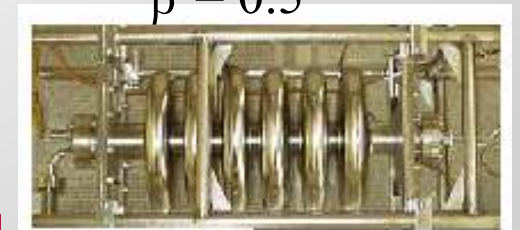
# Superconducting linac structures for radioactive beam accelerator (FRIB)



$\beta = 0.81$

$\beta = 0.61$

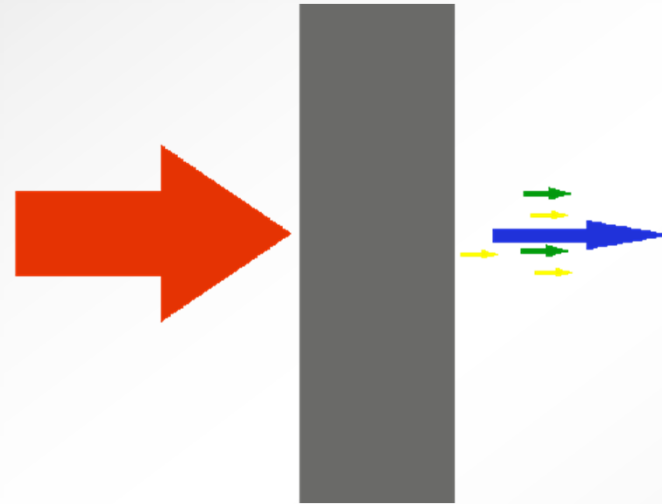
$\beta = 0.5$



US Particle Accelerator School



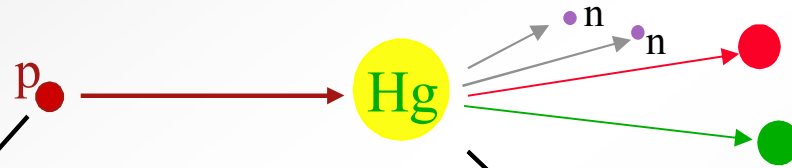
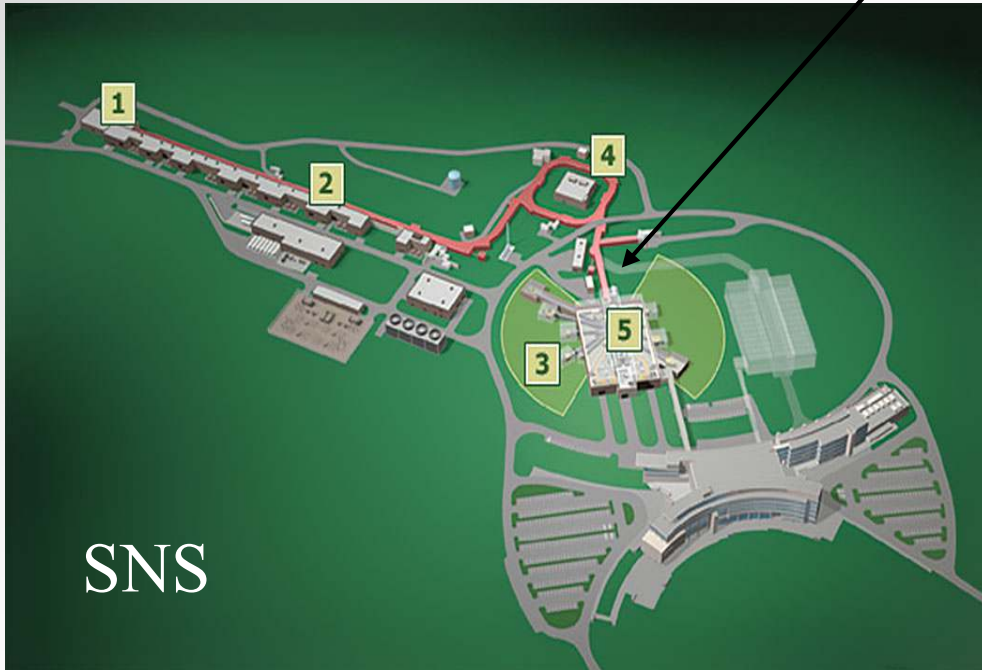
# Neutron science with accelerators



FOM: Neutrons/proton, neutron beam brightness



# Example: The Spallation Neutron Source at Oak Ridge National Laboratory



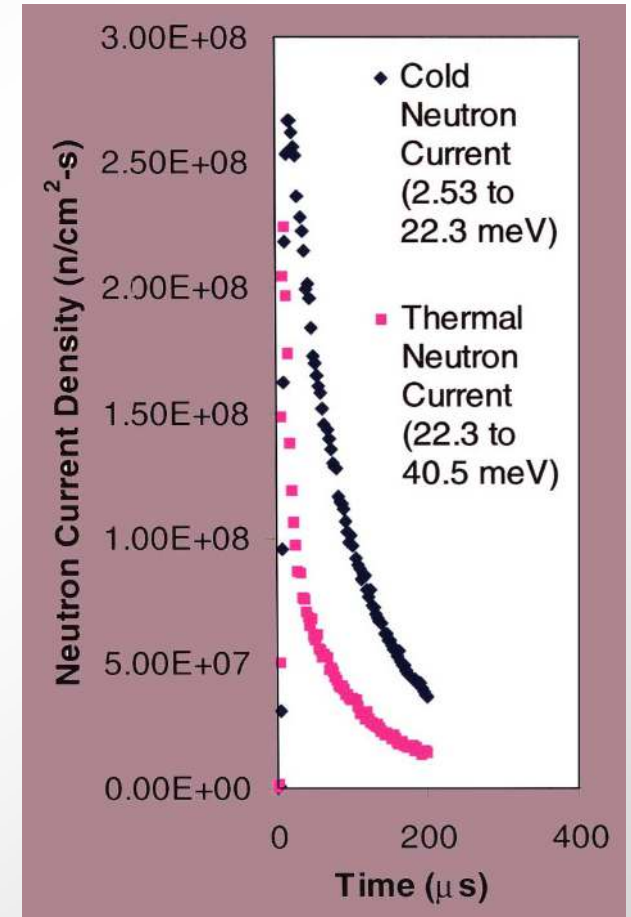
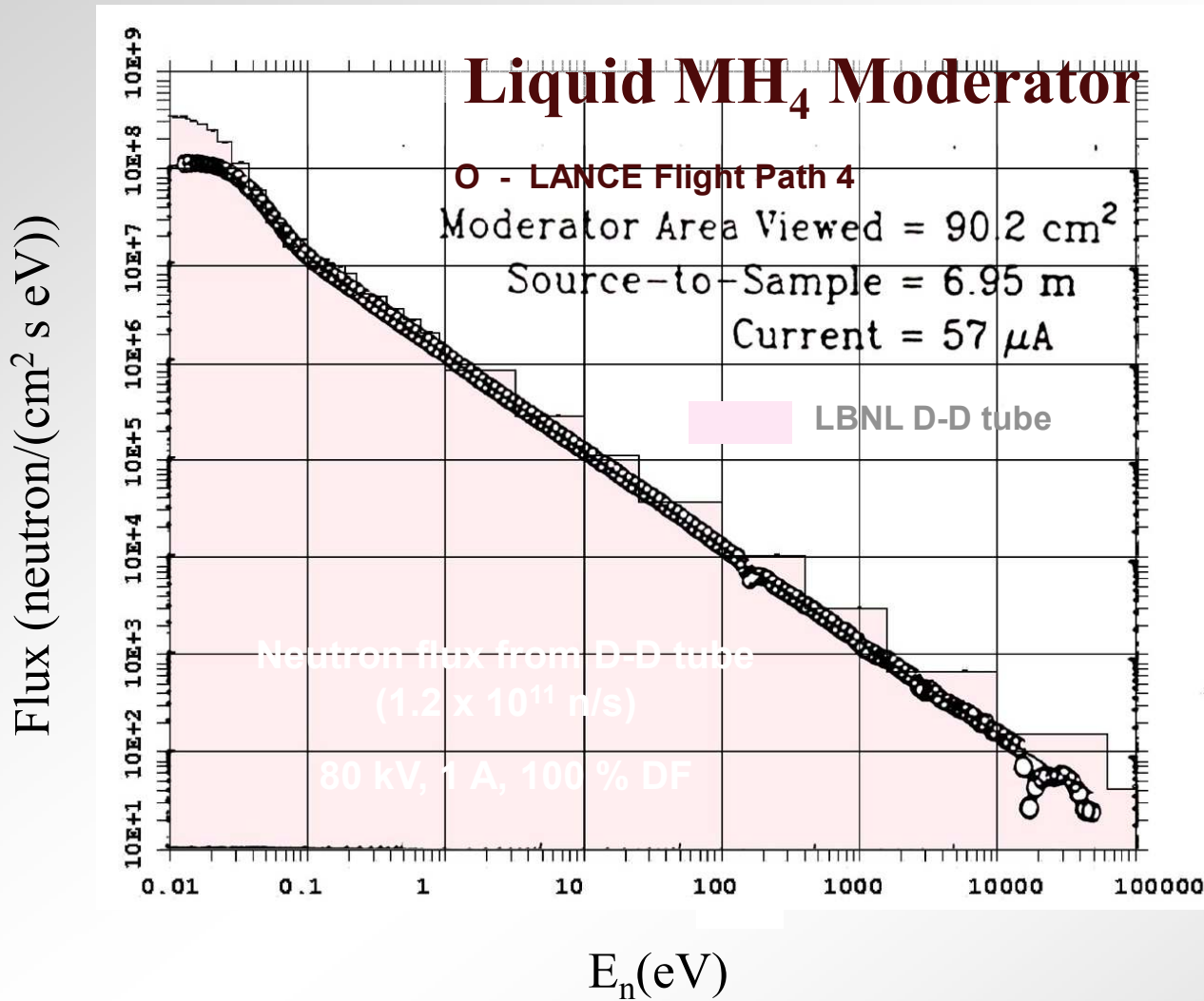
1 GeV, 35 mA of protons,  
6% duty factor

1 MW liquid Hg target  
 $>10^{17}$  n/sec





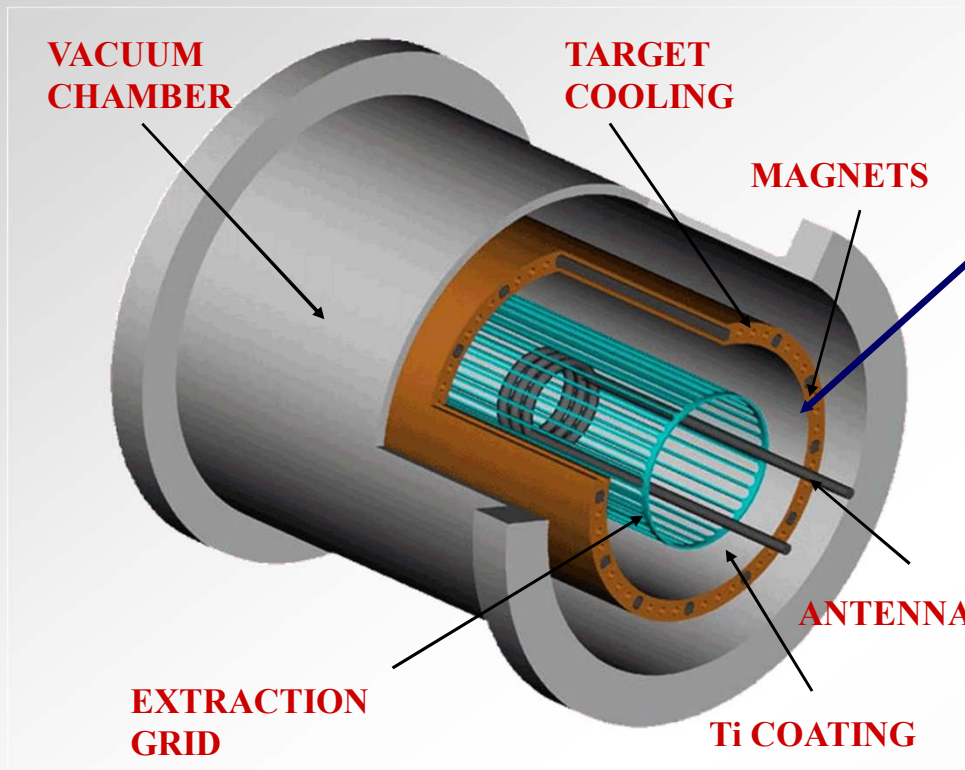
# Figures of Merit: Spectrum & time structure



○ The measured (circles) neutron flux v. neutron energy

Ref: Paul E. Koehler, Nucl. Instrum. Meth. A292, 541 (1990)

# Coaxial design increases target area in small volume source



## TARGET CHAMBER

Length	26cm
Diameter	28cm
Weight	40lb



For D-D neutron output  $\sim 1.2 \times 10^{12}$  n/s  
 For D-T neutron output  $\sim 3.5 \times 10^{14}$  n/s  
 @ 80 kW of beam, 10% d.f.

*Limiting parameter is power density on target*

1MW SNS (1 GeV, 60 Hz)

Protons per pulse  $\approx 10^{14}$

Neutrons per pulse  $\approx 20 \times 10^{14} = 2 \times 10^{15}$

Rate = 60 Hz  $\implies$  yield  $\approx 10^{17}$  n/s.

E/neutron = 1 MW/ $10^{17}$  n/s  $\approx 10^{-11}$  J/n

Overall efficiency for accelerator system  $\sim 2\%$

$\implies \sim 5 \times 10^{-10}$  J/n

D-T neutron tube (120kV, 1 A  $\implies 10^{14}$  n/s)

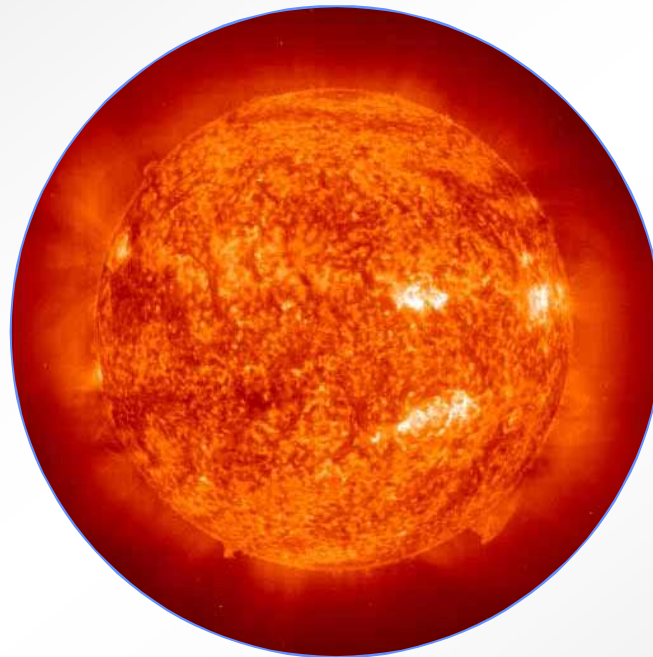
E/neutron  $\approx 120$  kW/ $10^{14}$  n/s  $\approx 10^{-9}$  J/n

DC power supply efficiency  $> 85\%$

$\implies \approx 10^{-9}$  J/n



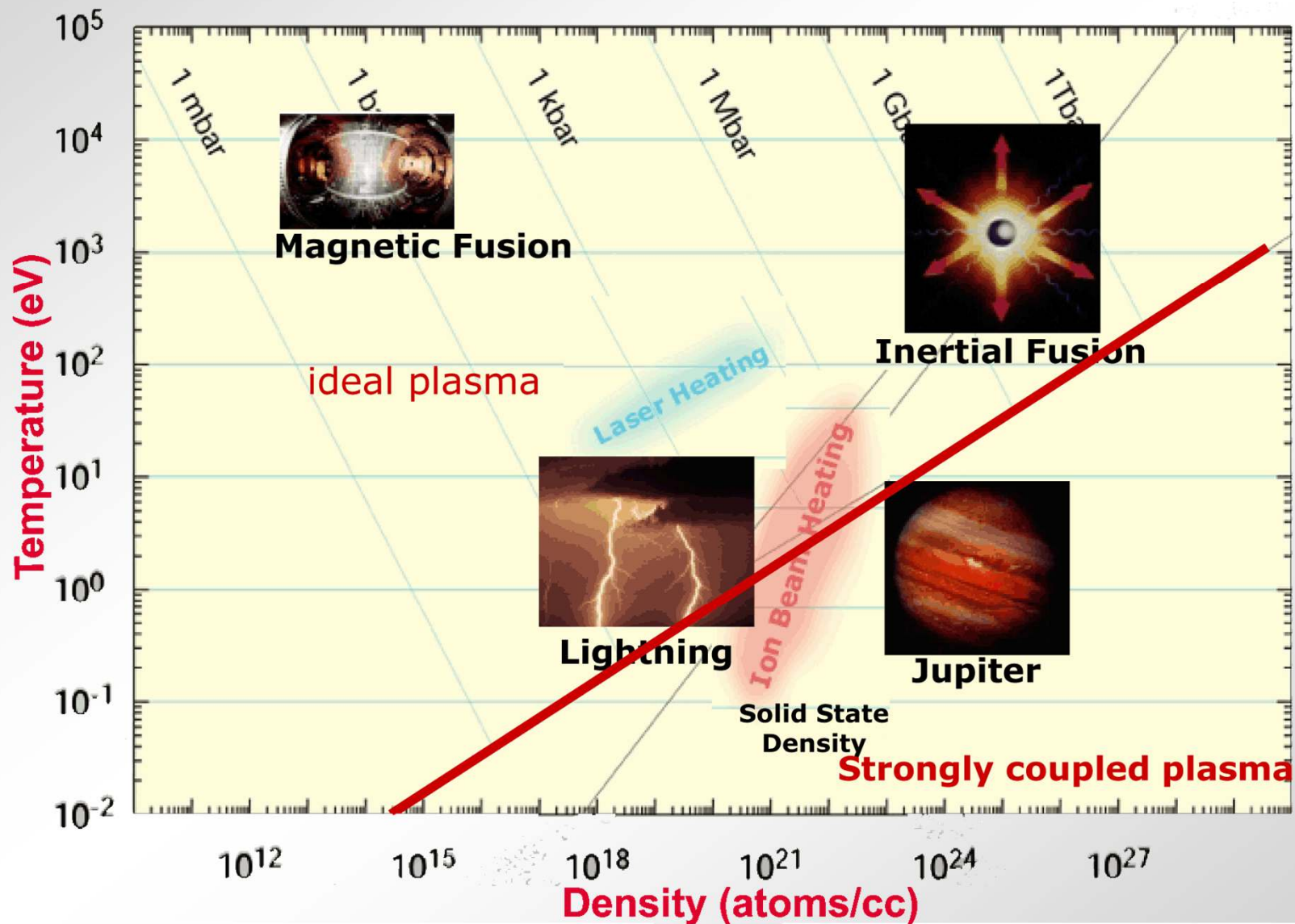
# Ion beams to produce fusion energy







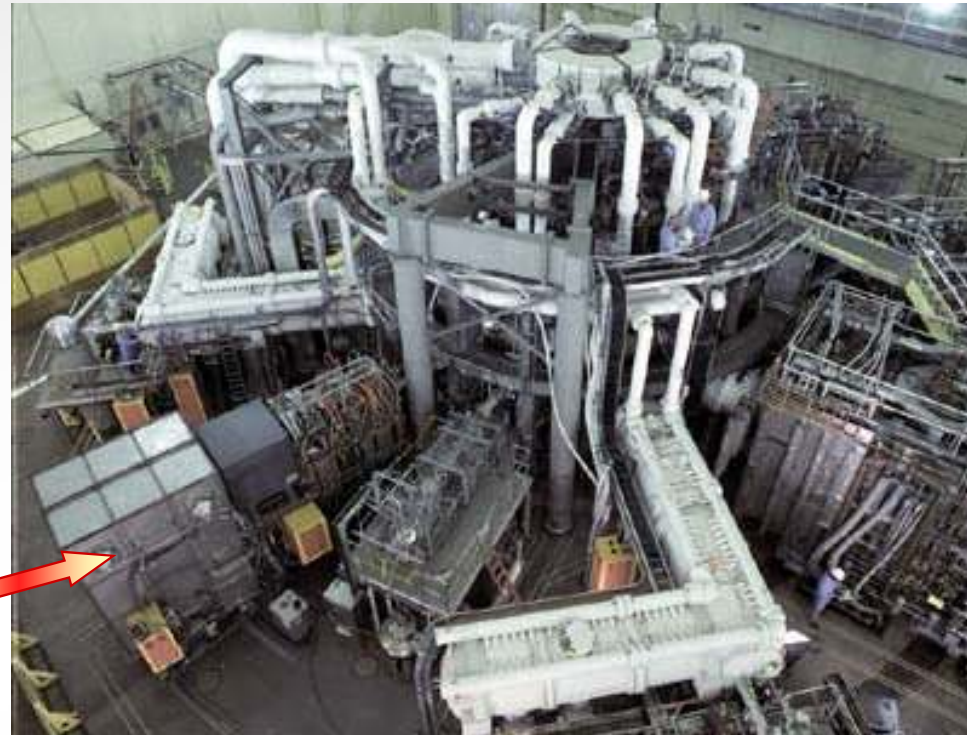
# Matter in extreme conditions can be driven by intense heavy ion beams





# Beams can heat fusion plasmas in tokomaks

- ❖ Example: neutral beams for TFTR at Princeton



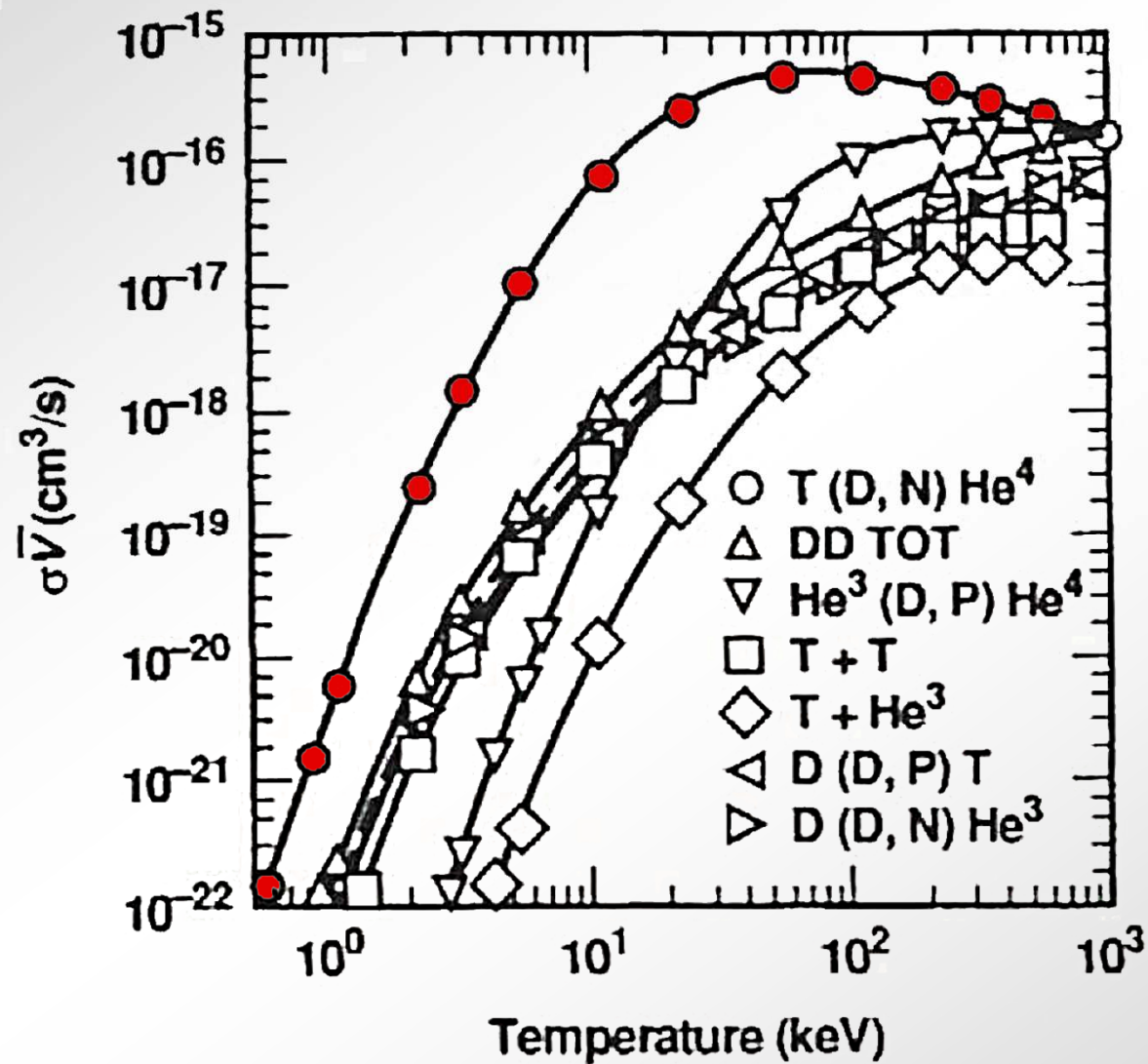
Neutral beam injectors

- ❖ ITER will require 60 MW of neutral beam heaters



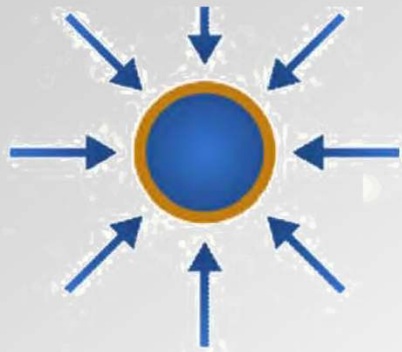


# Thermonuclear reaction rates





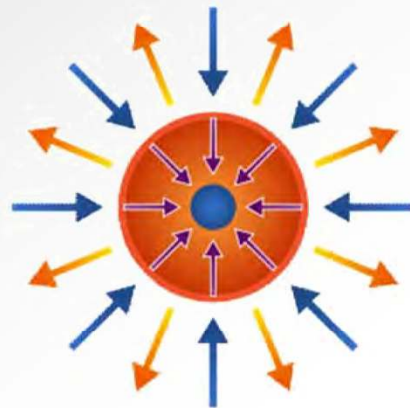
# How accelerators can produce fusion power



input energy quickly heats surface of fuel capsule

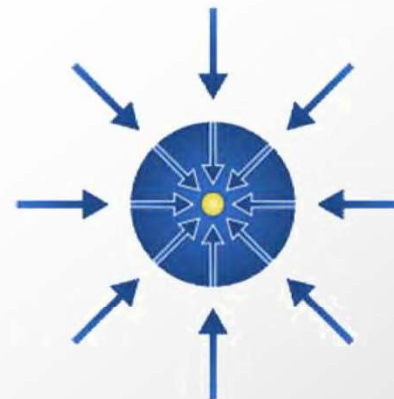
~10mg DT  
 $\rho \sim 0.5 \text{ mg/cm}^3$   
( $\rho \cdot r \sim 0.03\text{-}3 \text{ g/cm}^2$ )

Compression ratio  
up to 30:1



fuel is compressed isentropically by  
rocket-like blowoff of hot surface material

compressed fuel core ("hotspot") reaches  
density and temperature needed for  
ignition



$\rho \sim 100 \text{ g/cm}^3$  (hotspot)  
 $T \sim 5\text{-}12 \text{ keV}$   
( $\rho \cdot r \sim 0.2\text{-}0.5 \text{ g/cm}^2$ )

$\rho \sim 400\text{-}800 \text{ g/cm}^3$  (fuel)  
 $T \ll 5 \text{ keV}$

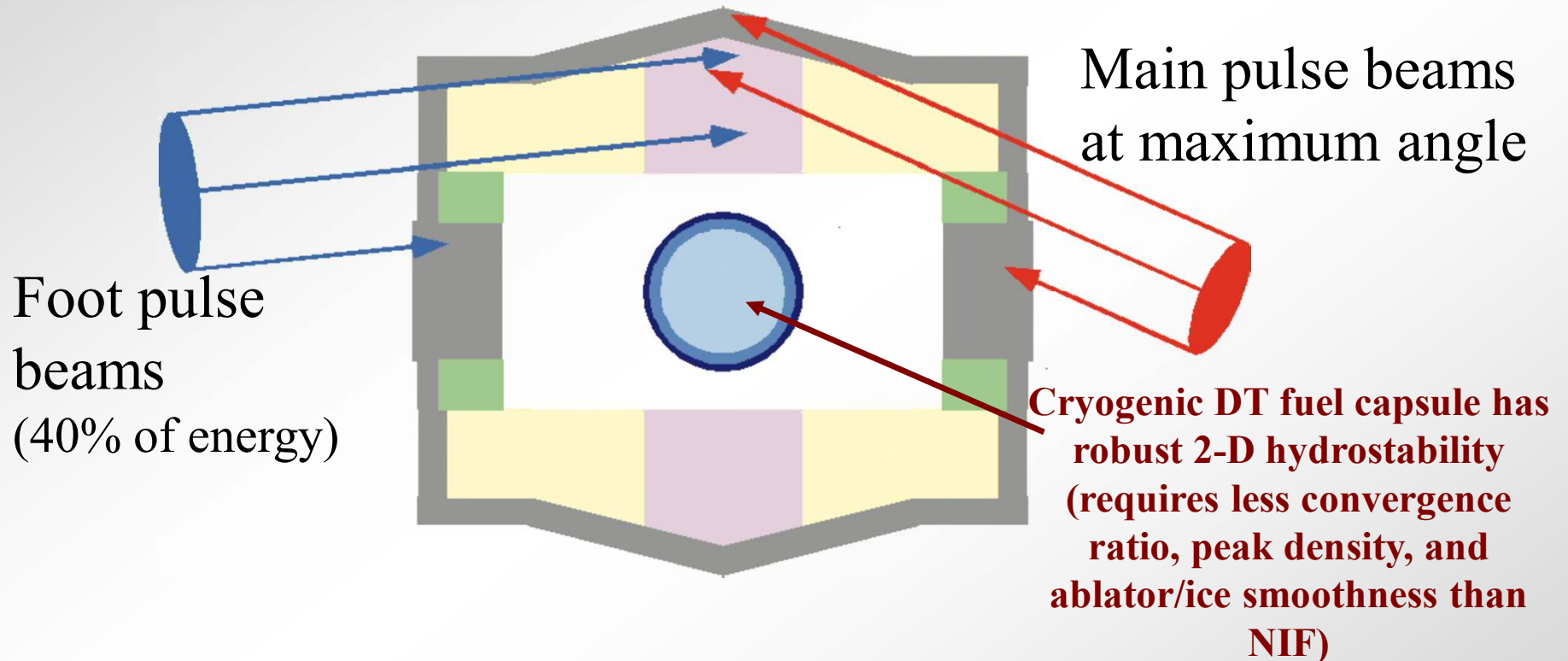
thermonuclear burn spreads quickly through compressed fuel



0.5-2 GJ  
~50ps



# Indirect drive: Target design is a variation of the distributed radiator target (DRT)

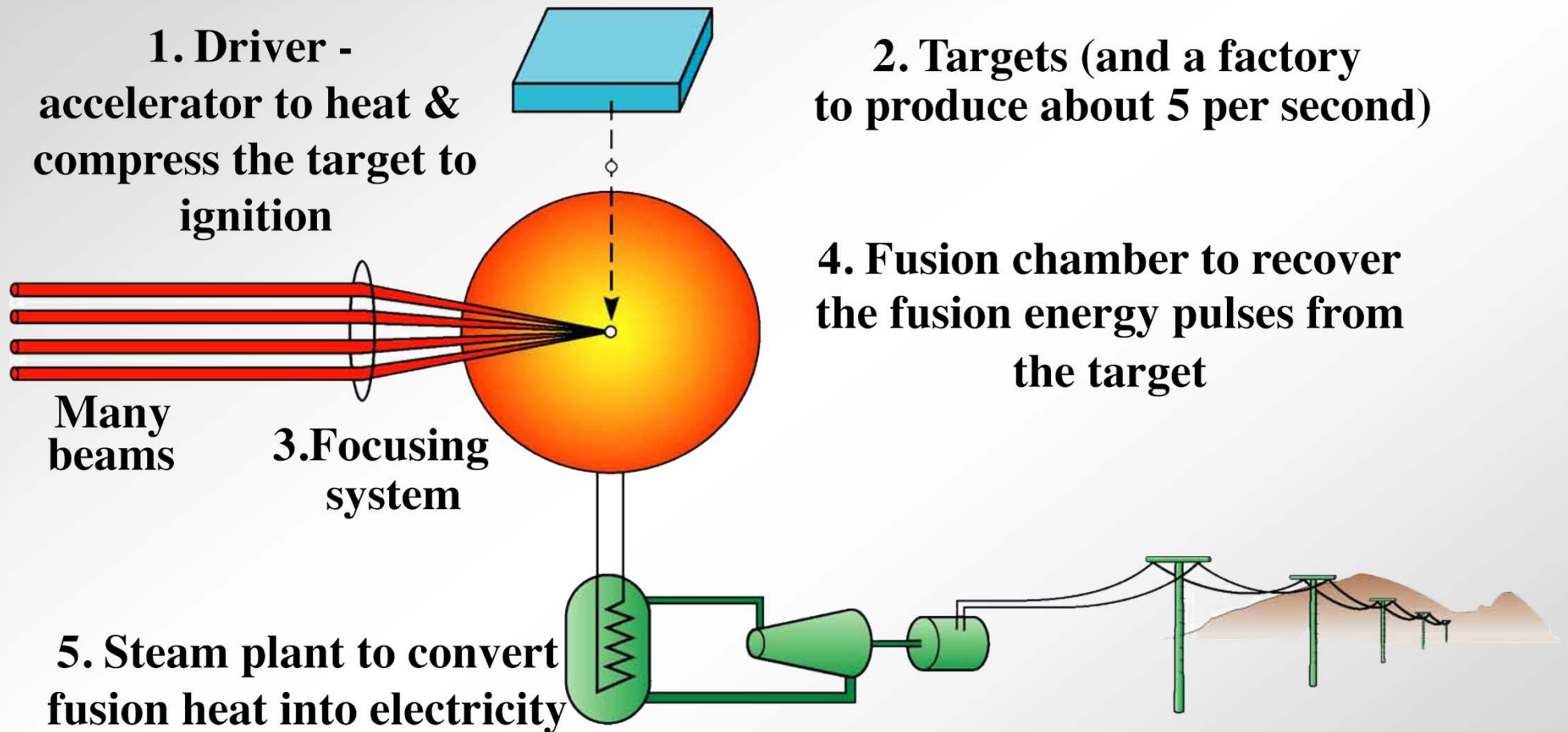


*New design allows beams to come in from larger angle,  $\sim 24^\circ$  off axis.*

*Yield = 400 MJ, Gain = 57 at  $E_{driver} = 7$  MJ*



# The inertial fusion power plant





# Beam requirements for HIF

- ❖ Representative set of parameters for indirect-drive targets
  - ~ 5 Megajoules of beam energy
  - ~500 Terawatts of beam power ==> tens of kA
  - beam pulse length ~ 10 ns
  - range 0.02 - 0.2 g/cm<sup>2</sup>
  - focus such a large beam to a spot of ~1-5 mm radius
  - desired focal length ~6 m (maximum chamber size)
- ❖ Basic requirements ==> certain design choices
  - parallel acceleration of multiple beams
  - acceleration of needed charge in a single beam is uneconomical
  - emittance required to focus single large beam extremely difficult

*Requires a new class of accelerator*



# The new radiation science: The Ultra-fast & Ultra-bright

## “Big Questions ”

Can we image single molecules?

Can we make molecular movies of chemical reactions?

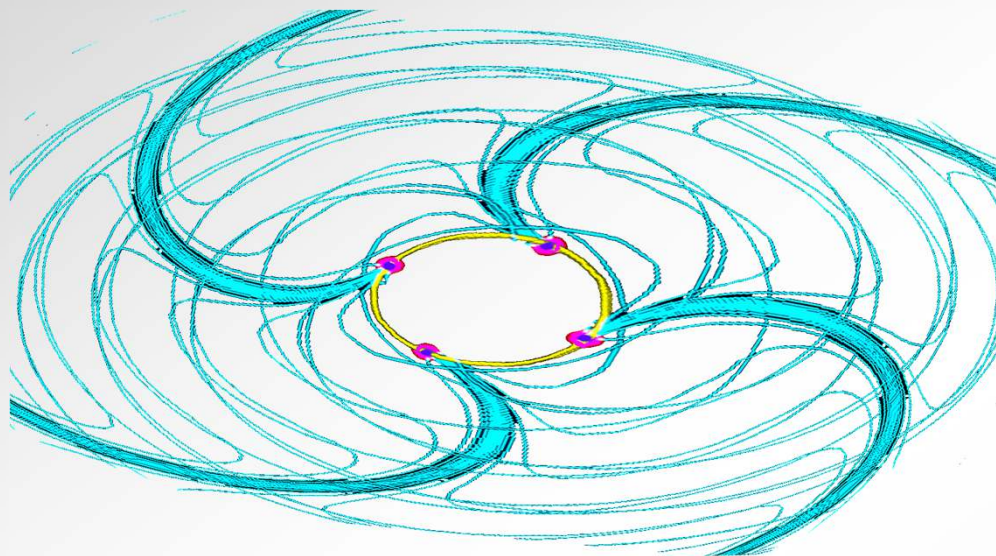
Can we “stop electrons in their tracks”?



# Synchrotron radiation science (~ 70 facilities world-wide)

## Synchrotron light source

*Calculated electric field lines from 4 bunches in circular orbit*



*In practice the vacuum chamber cuts out all but the 1/γ cone*

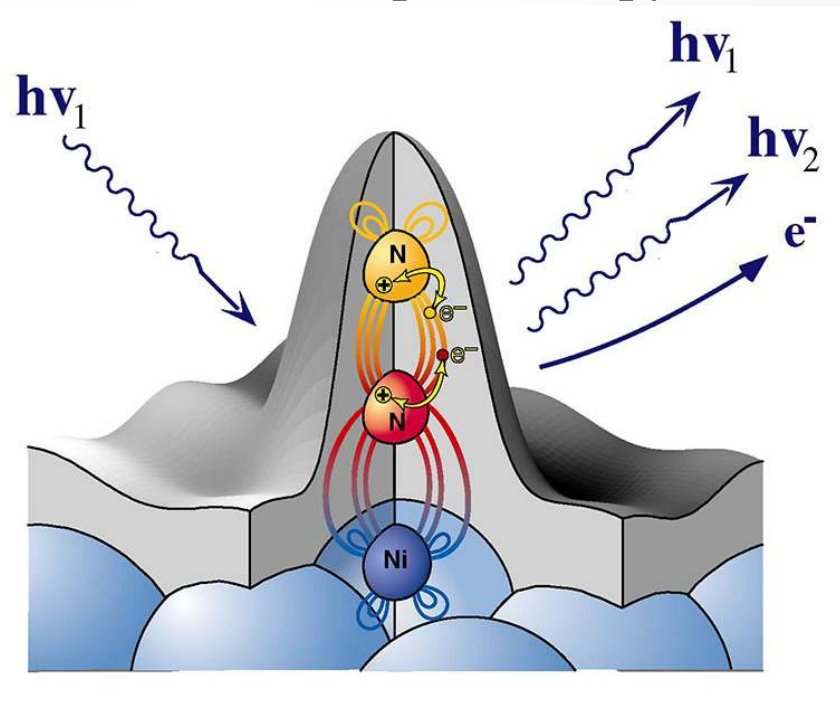
FOM: Brilliance v.  $\lambda$

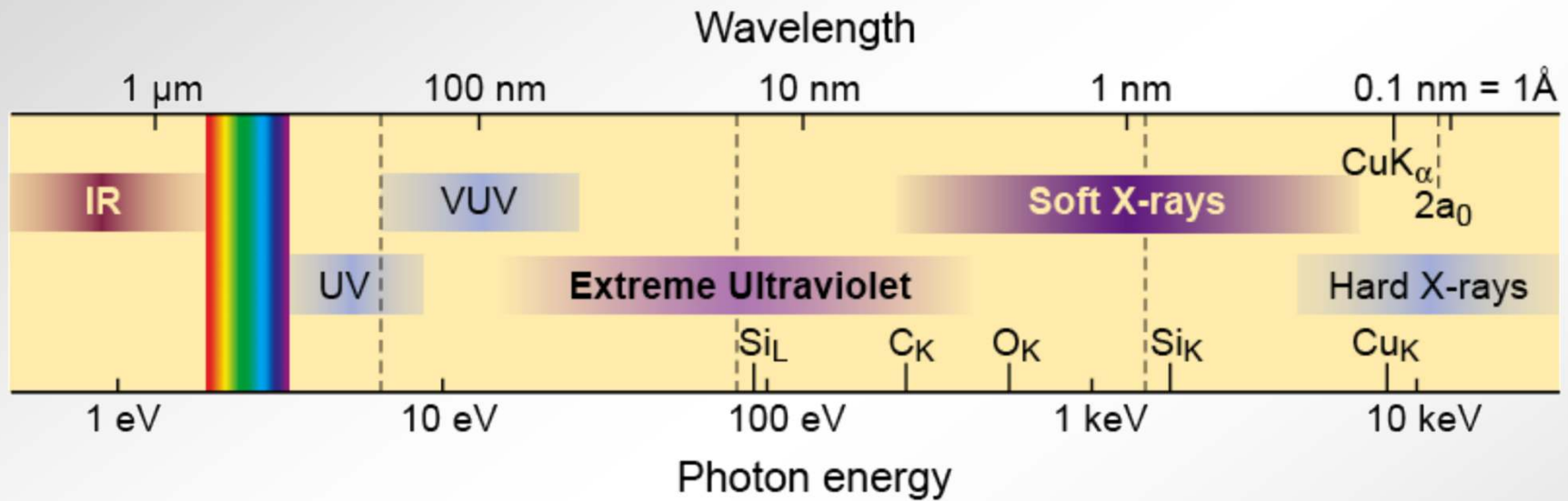
$$B = \text{ph/s/mm}^2/\text{mrad}^2/0.1\% \text{BW}$$

*These facilities enable fixed target experiments with photons*

### □ Science with X-rays

- Microscopy
- Spectroscopy





- See smaller features
- Write smaller patterns
- Elemental and chemical sensitivity

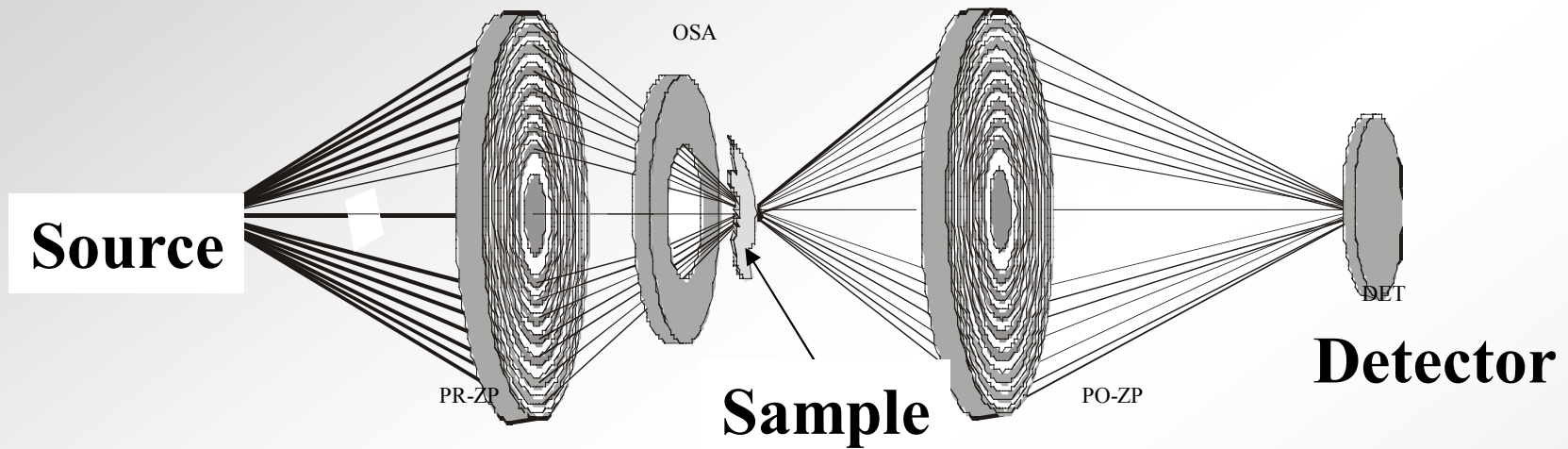


Figure . Optical scheme of TwinMic.

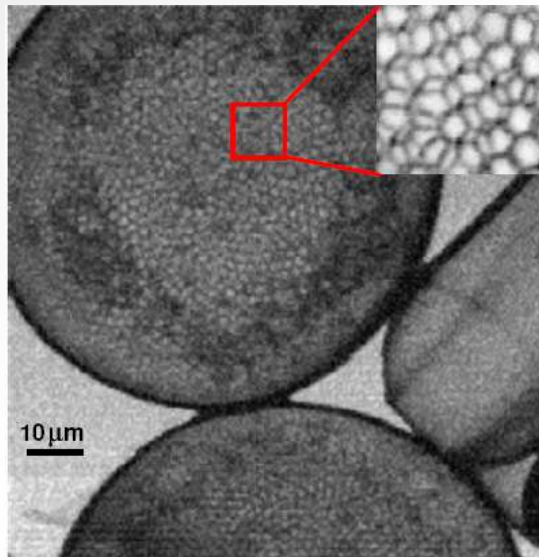


Figure 3. Scanning mode

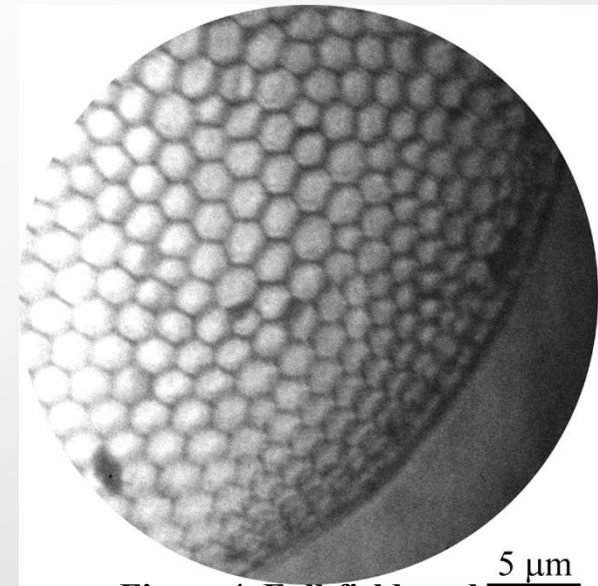


Figure 4. Full-field mode.



Does the tracheal system limit the size of insects?

Research\* at the Argonne Advanced Photon Source (APS) explains what limits size in beetles: the constriction of tracheal tubes leading to legs.

\* Alexander Kaiser, C. Jaco Klok, John J. Socha, Wah-Keat Lee, Michael C. Quinlan, and Jon F. Harrison, “Increase in tracheal investment with beetle size supports hypothesis of oxygen limitation on insect gigantism,” [Proc. Nat. Acad. Sci. USA \*\*104\*\*\(32\), 13198 \(August 7, 2007\)](#).





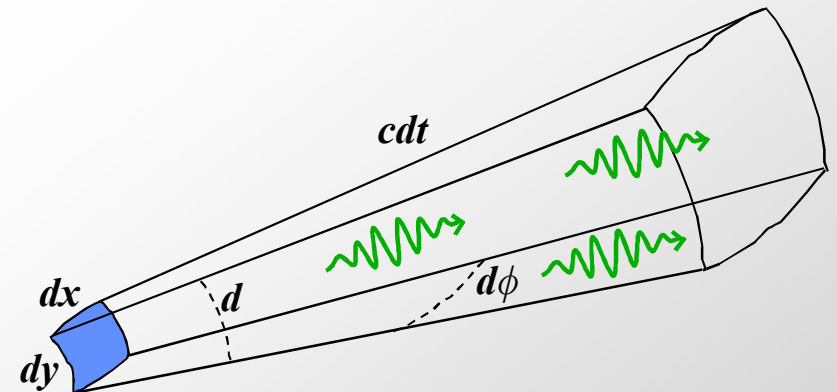


# Brightness of a Light Source

- ❖ Brightness is a principal characteristic of a particle source
  - Density of particle in the 6-D phase space
- ❖ Same definition applies to photon beams
  - Photons are bosons & the Pauli exclusion principle does not apply
  - Quantum mechanics does not limit achievable photon brightness

$$\text{Brightness} = \frac{\# \text{ of photons in given } \Delta\lambda/\lambda}{\text{sec, mrad } \theta, \text{ mrad } \varphi, \text{ mm}^2}$$

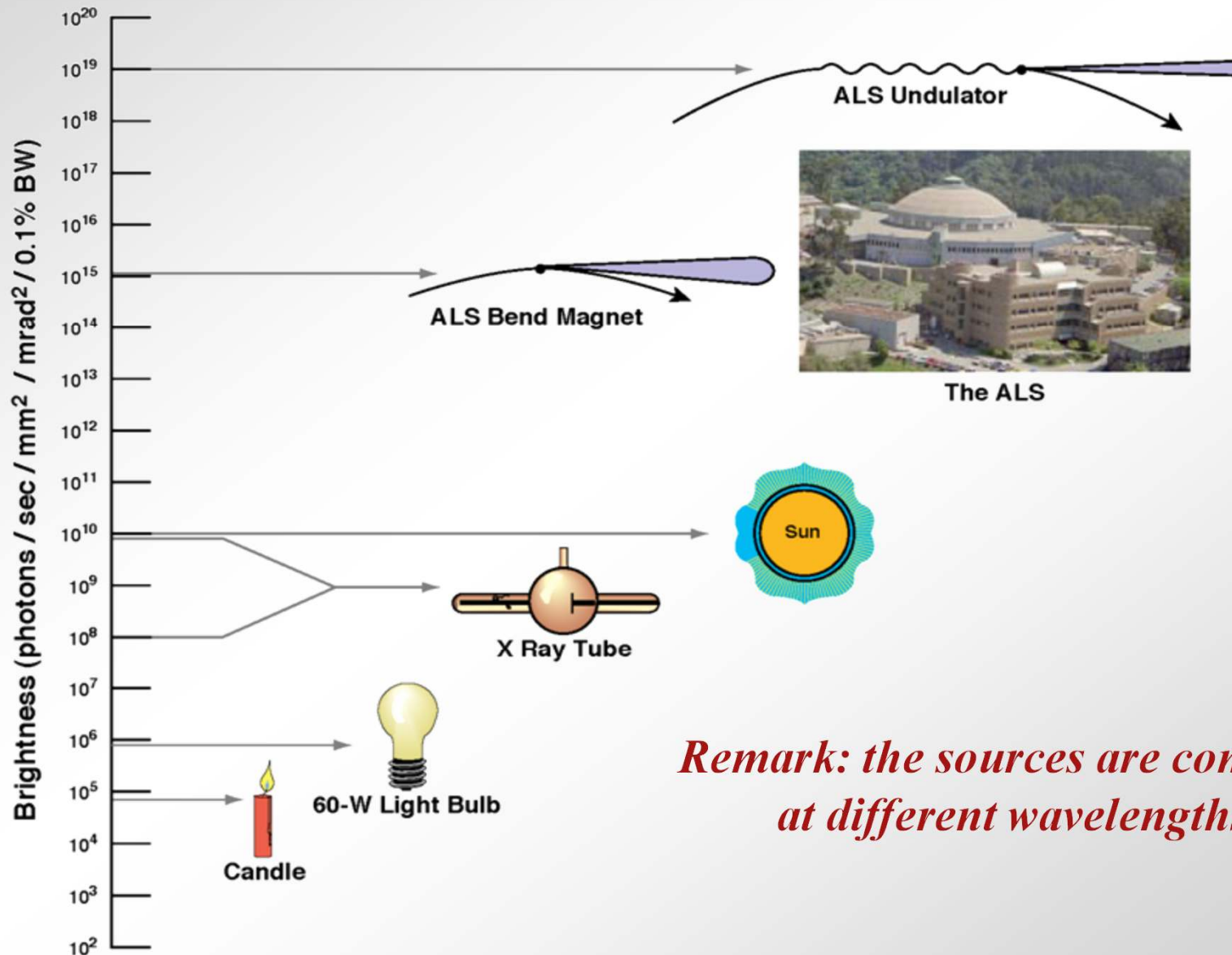
$$\text{Flux} = \frac{\# \text{ of photons in given } \Delta\lambda/\lambda}{\text{sec}}$$



$$\text{Flux} = \frac{dN}{d\lambda} = \int \text{Brightness } dS d\Omega$$



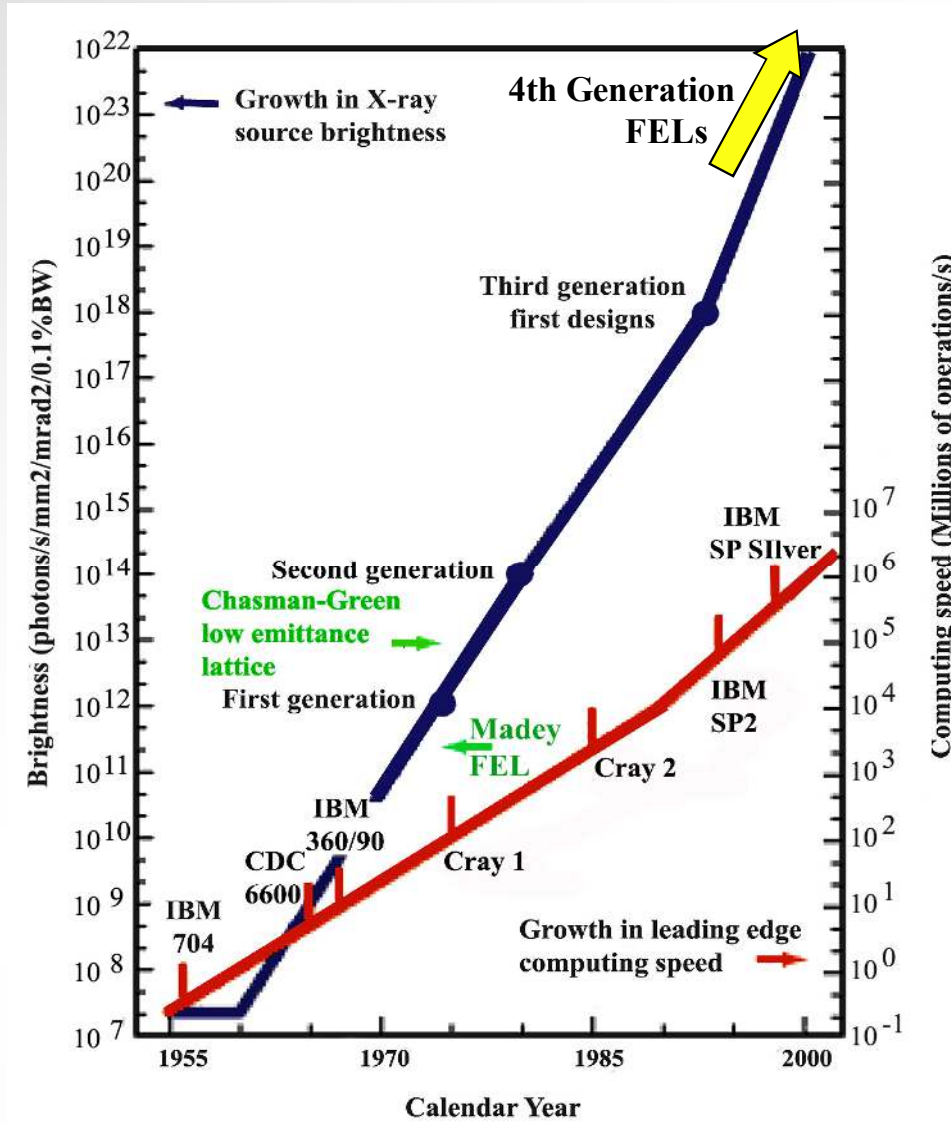
# How bright is a synchrotron light source?



*Remark: the sources are compared at different wavelengths!*



# Progress in X-ray source brightness



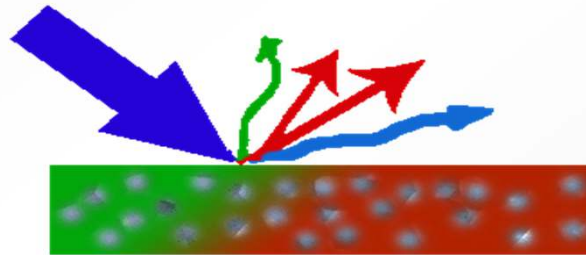
*Studying ultra-fast processes requires another great invention: FEL*



# Grand challenge science with X-rays

## Two general modes of experiments

- Image molecular structures with *atomic resolution*
  - “Diffract before destroy”
- Unprecedented studies of dynamics parameters combining spectroscopy & diffraction using X-rays
  - Typically “pump-probe”



### Figures of Merit:

Brilliance v.  $\lambda$  ( $B = \text{ph/s/mm}^2/\text{mrad}^2/0.1\% \text{BW}$ )

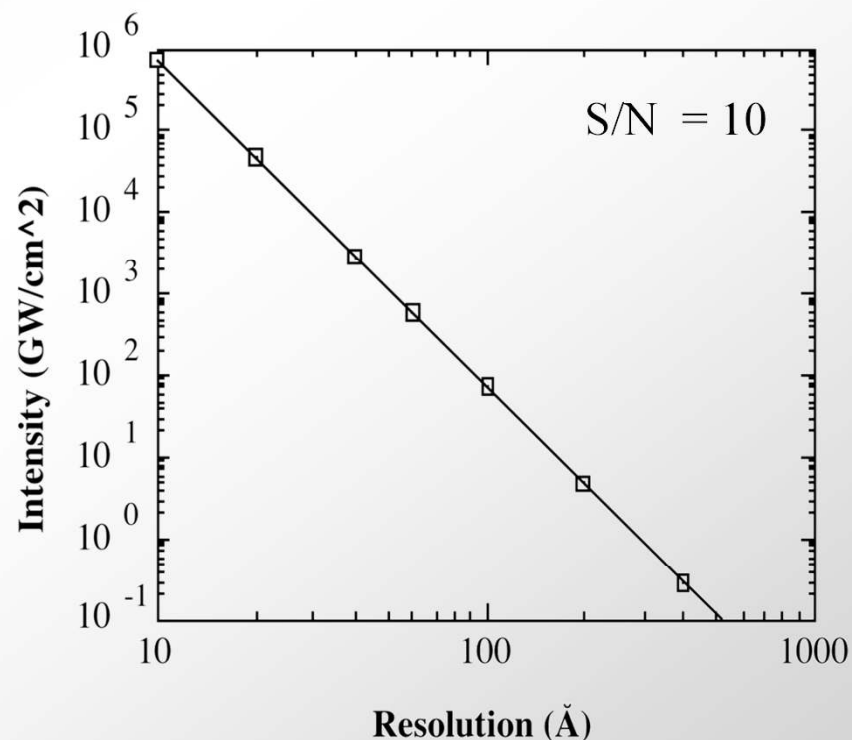
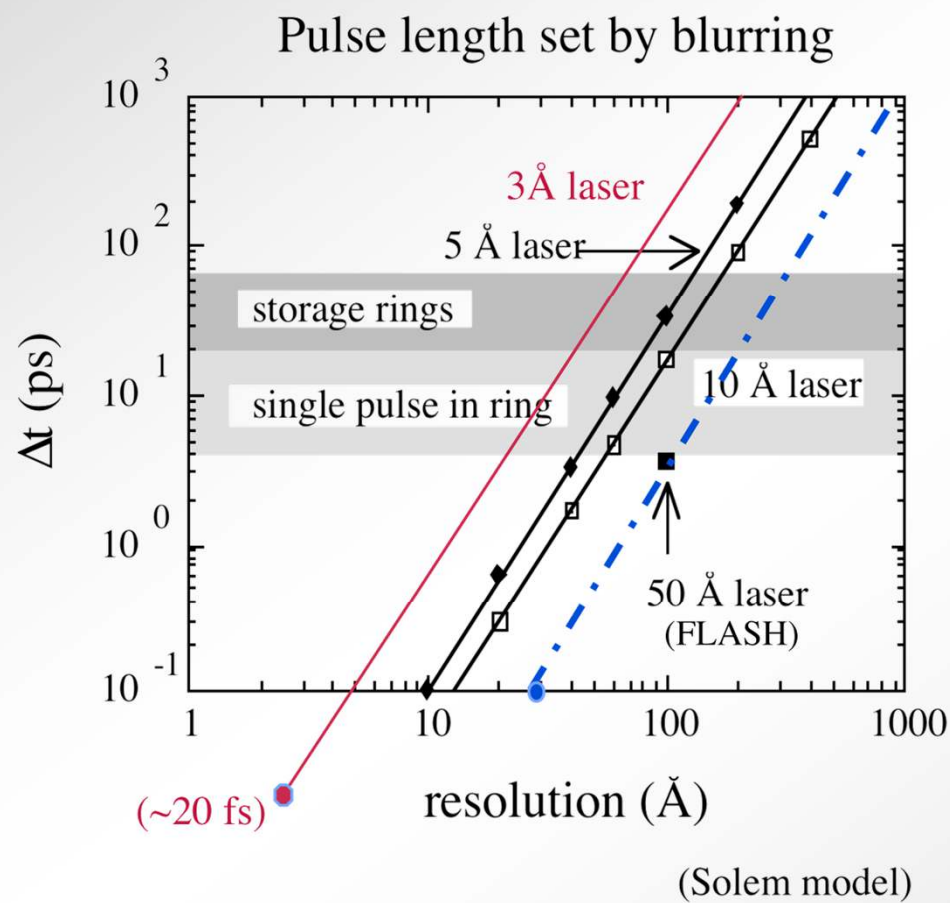
Time structure of x-ray pulses



# Diffract before destroy: Ultra-fast imaging => Sub-100 fs & >10 GW pulses

## ❖ Simple calculation of molecular imaging

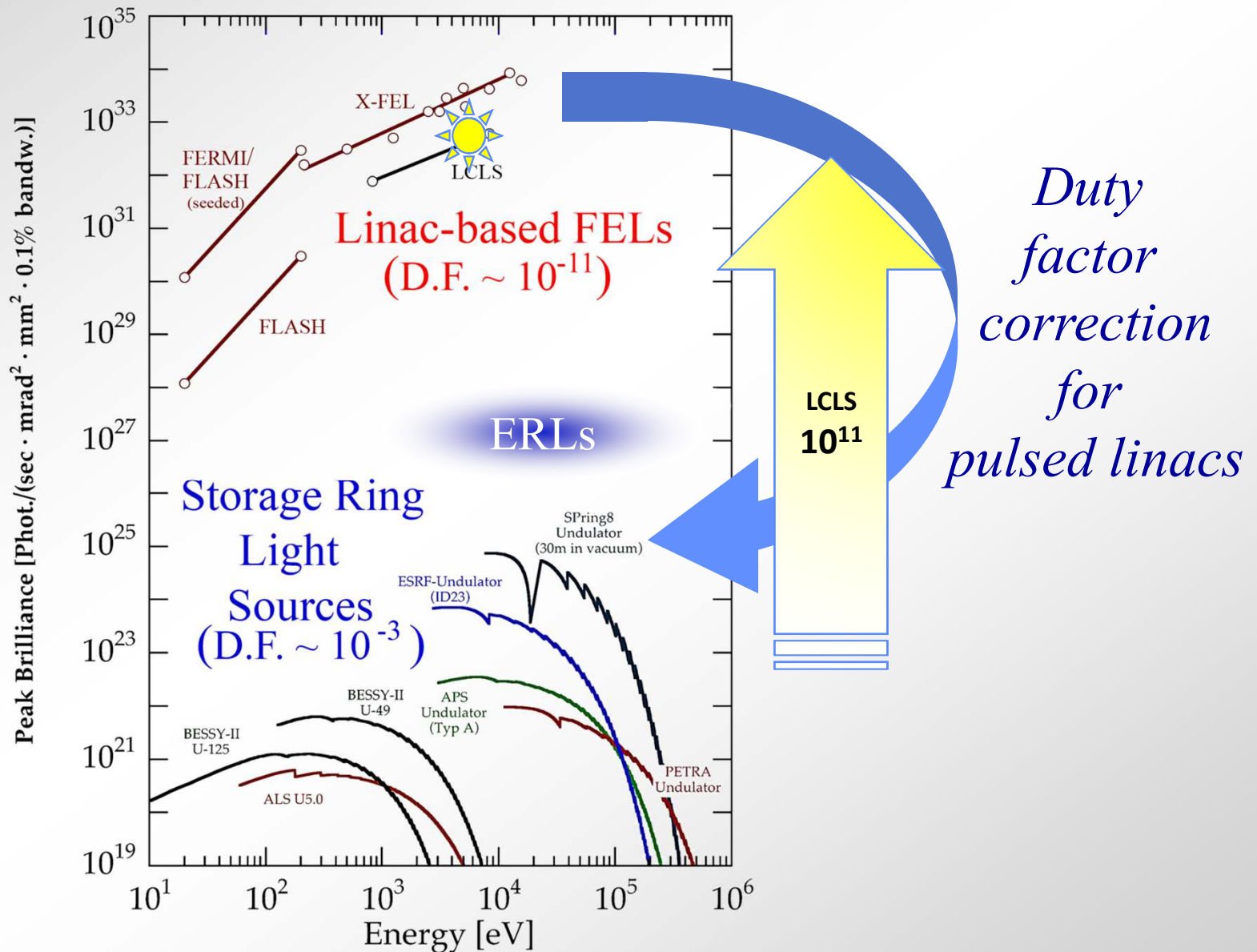
- Updated from “SLAC-lite” calculations (Barletta, 1993)

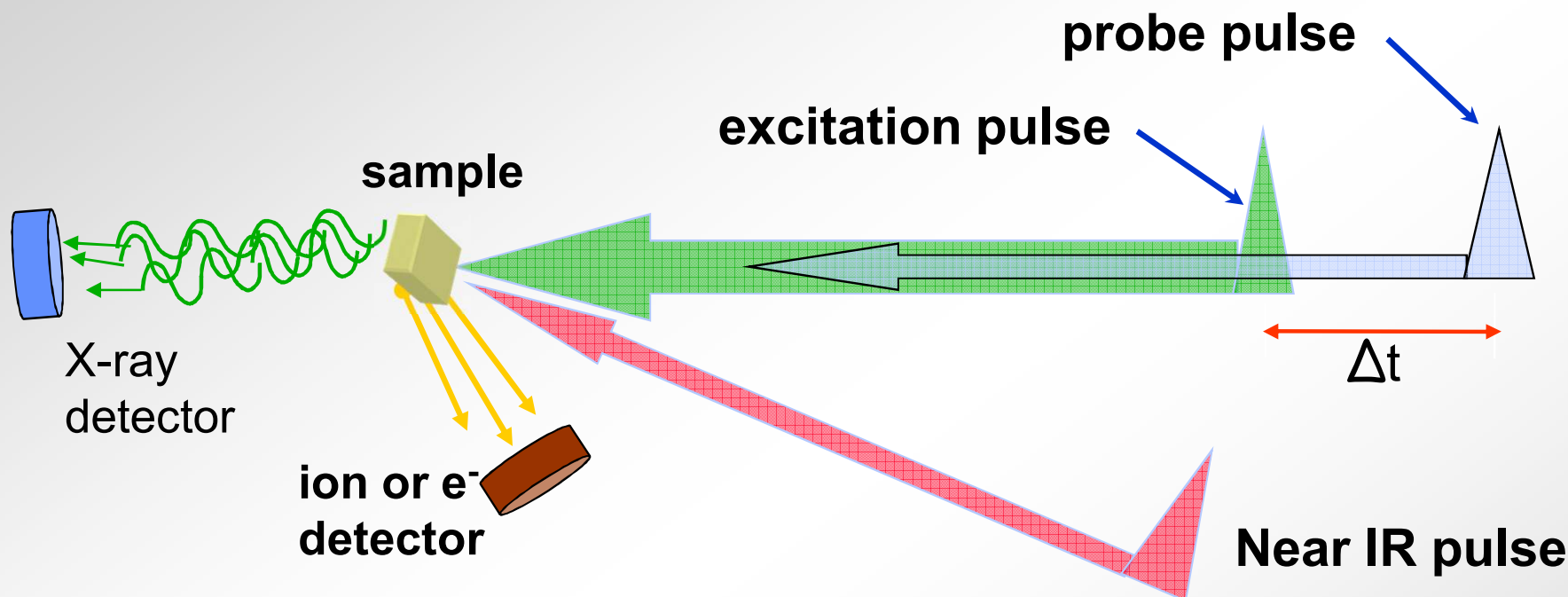






# Figure of Merit: Light source brilliance v. photon energy



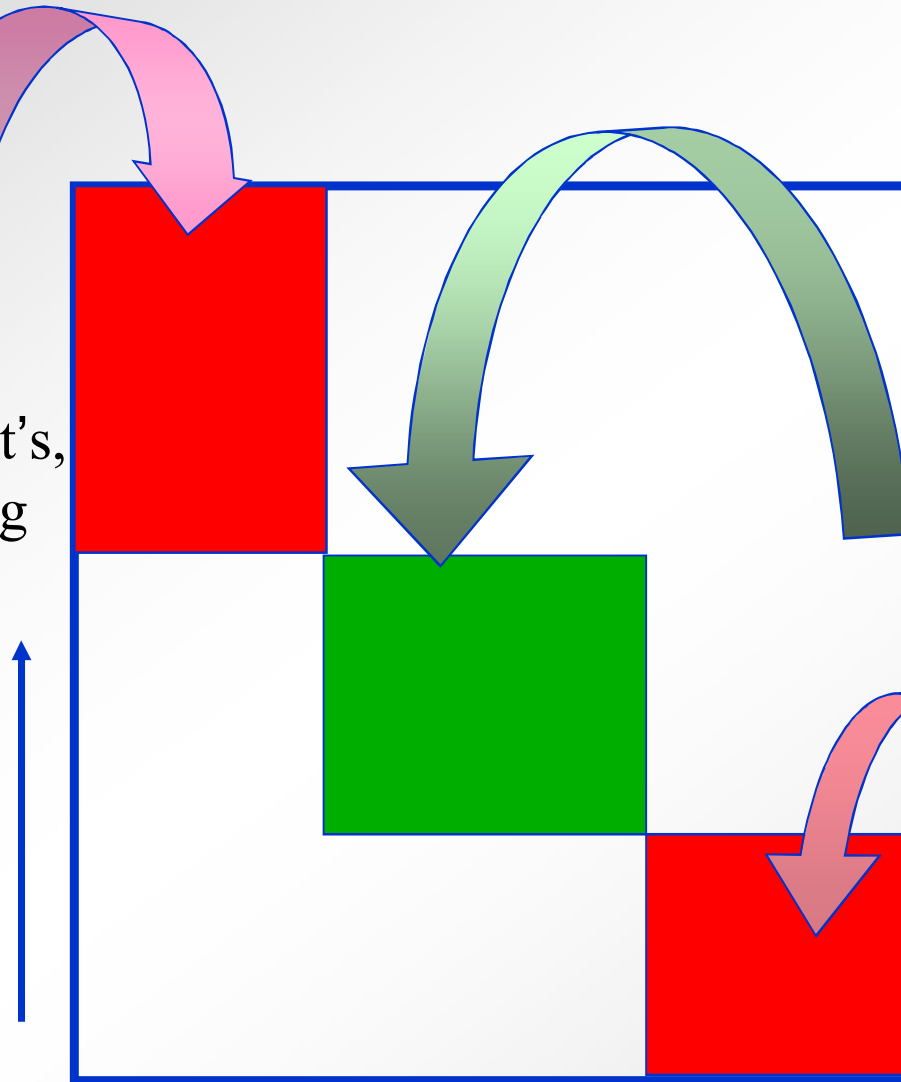


- Pulses can be x-rays, VUV, electrons or ions
- Control/measure  $\Delta t$  with a resolution  $\ll$  x-ray pulse duration
  - Possibly as small as 300 attoseconds

MHz-GHz, nJs

Limited by acoustic velocities in samples, good for counting expt's, photoemission imaging

Repetition rate

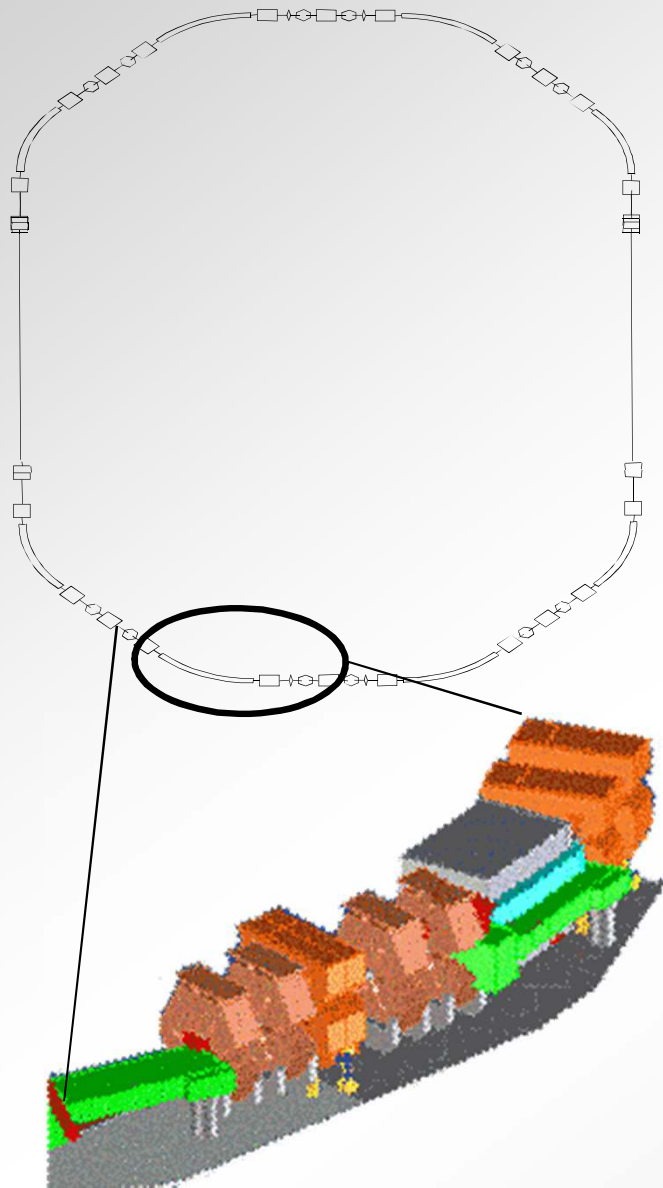


1 kHz-1 MHz,  $\mu$ Js  
Ideal match to ultrafast lasers & sample considerations, single photon regime

10-100Hz, mJs,  
Limited by sample damage, many high field effects

Pulse energy

# Approach 1: Diffraction limited storage rings



## ❖ 100 x brighter than existing rings

- Ideal for structural studies
- Extremely stable, Many simultaneous users

*The U.S. needs a diffraction limited,  
hard X-ray source to remain competitive  
BUT cannot access ultra-fast processes*

## ❖ Pulse length in rings (20 - 50 ps) is set by

- Natural energy spread
- Coherent synchrotron radiation
- Instabilities

*These effects take many revolutions  
to spoil the beam*

*==> Discard the beam after using*



# Approach 2: Energy Recovery Linacs (Hard X-rays $\Rightarrow$ $\sim 5$ GeV electrons)

**Synchrotron light source**  
(pulsed incoherent X-ray emission)

Pulse rates – kHz  $\Rightarrow$  MHz

X-ray pulse duration  $\sim 1$  ps

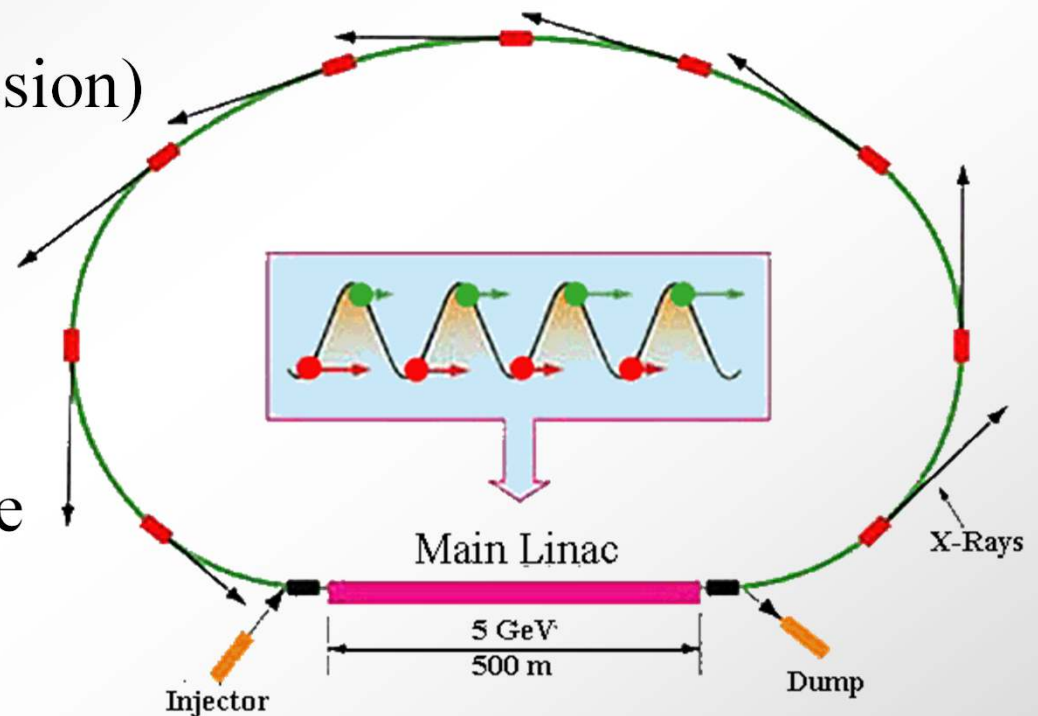
High average e-beam brilliance  
& e-beam duration  $\sim 1$  ps

$\Rightarrow$  One pass through ring

$\Rightarrow$  Recover beam energy

$\Rightarrow$  High efficiency

$\Rightarrow$  **Superconducting RF**  
**optimized for CW operation**



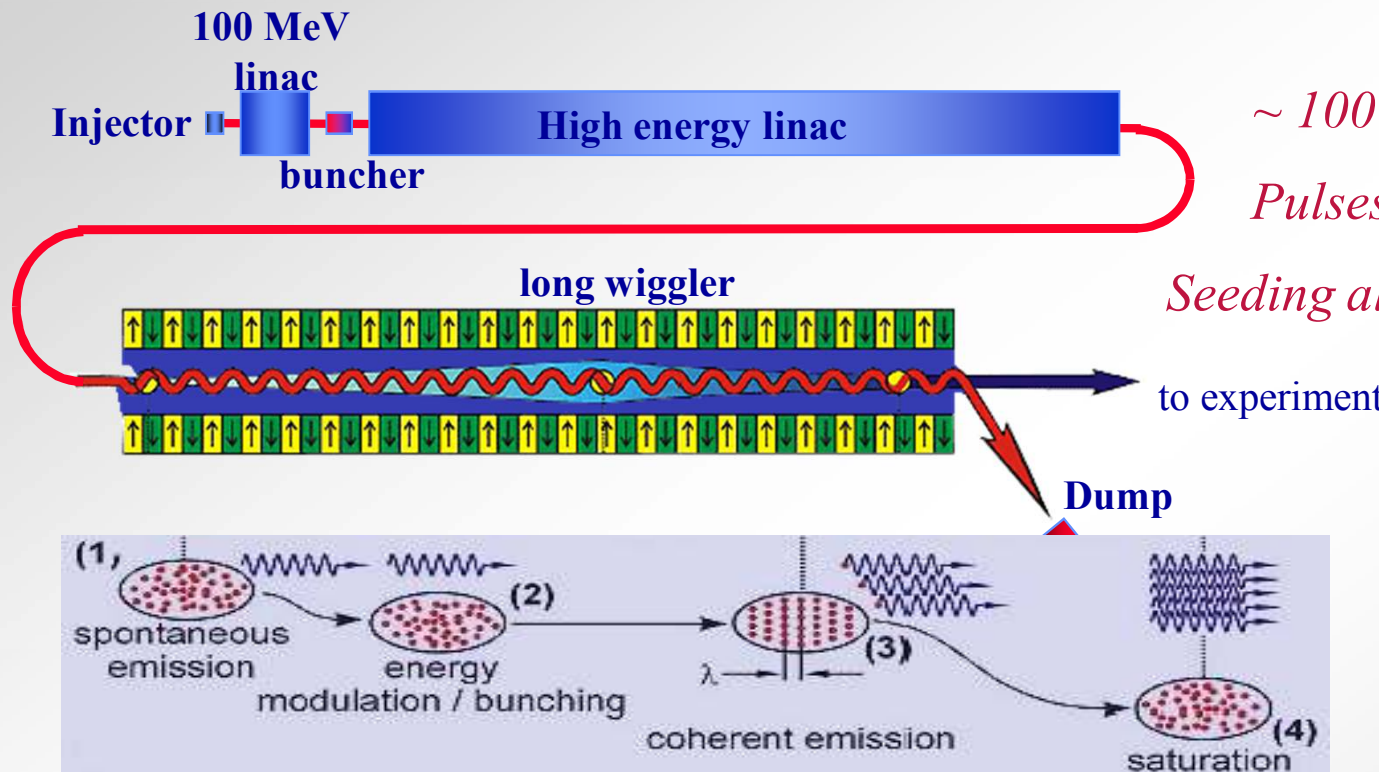
*Pulse duration &  $\Delta E$  limited  
( $> 50$  fs at 0.1% bandwidth)  
by coherent synchrotron radiation  
in the arcs*





# Approach 3: fs pulses & highest brightness

## Coherent emission ==> FEL



**For SCRF linacs**

*~ 100 kHz to >1 MHz practical*

*Pulses length of ~ 1 fs practical*

*Seeding allows for full phase coherence*

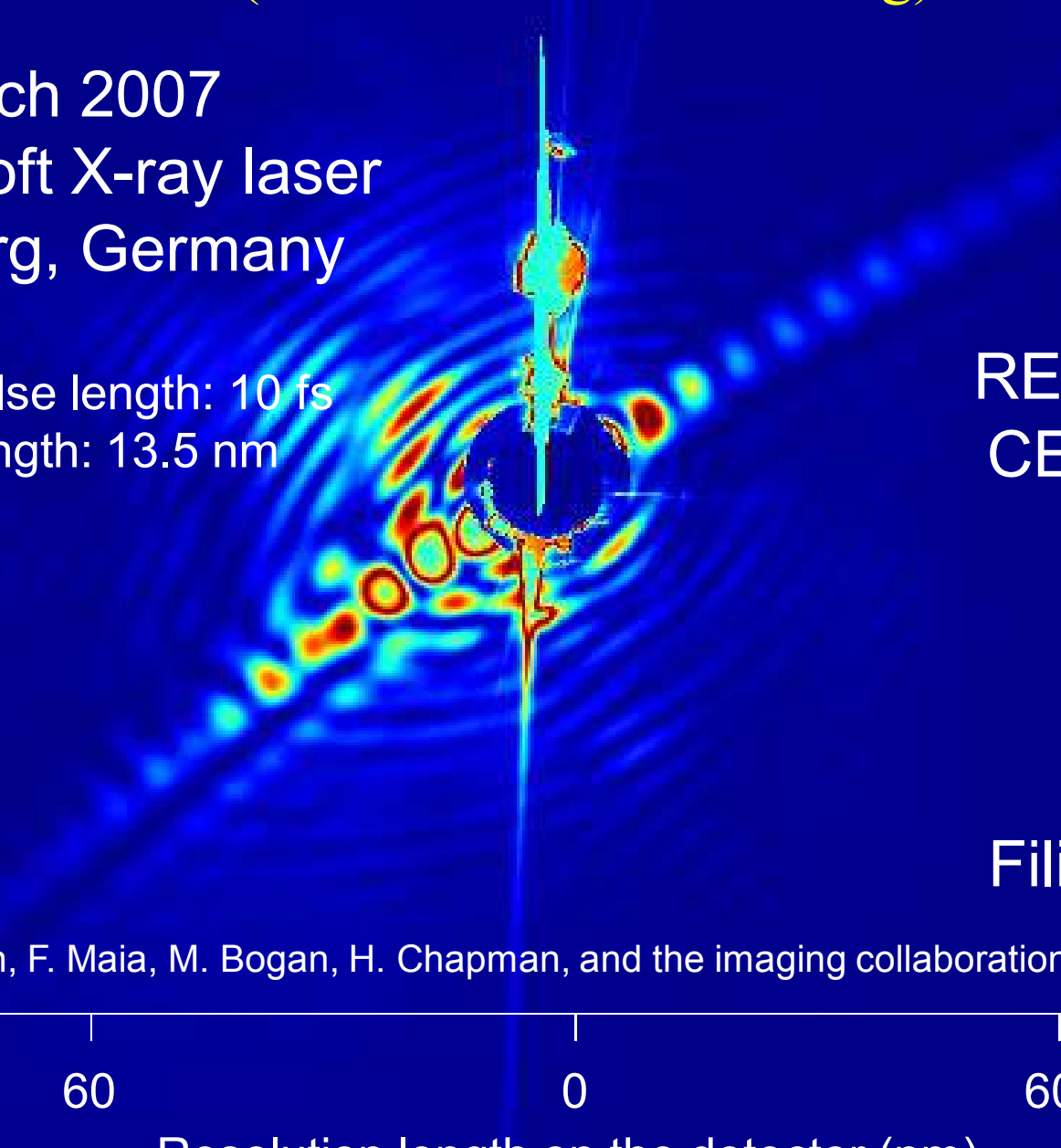
$$\rho = \frac{1}{\gamma} \left( \frac{a_w \omega_p}{4 c k_w} \right)^{2/3} \propto \frac{I^{1/3} B^{2/3} \lambda_w^{4/3}}{\gamma}$$

*High rep rate FEL meets the challenge of the “Big Questions”*  
*IF we know how to seed the FEL*

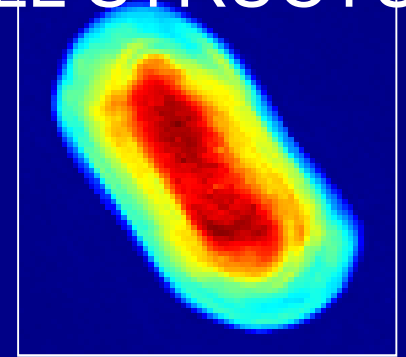
# First X-ray diffraction image of a live picoplankton (FLASH FEL in Hamburg)

March 2007  
FLASH soft X-ray laser  
Hamburg, Germany

FLASH pulse length: 10 fs  
Wavelength: 13.5 nm



RECONSTRUCTED  
CELL STRUCTURE



Filipe Maia, Uppsala

J. Hajdu, I. Andersson, F. Maia, M. Bogan, H. Chapman, and the imaging collaboration

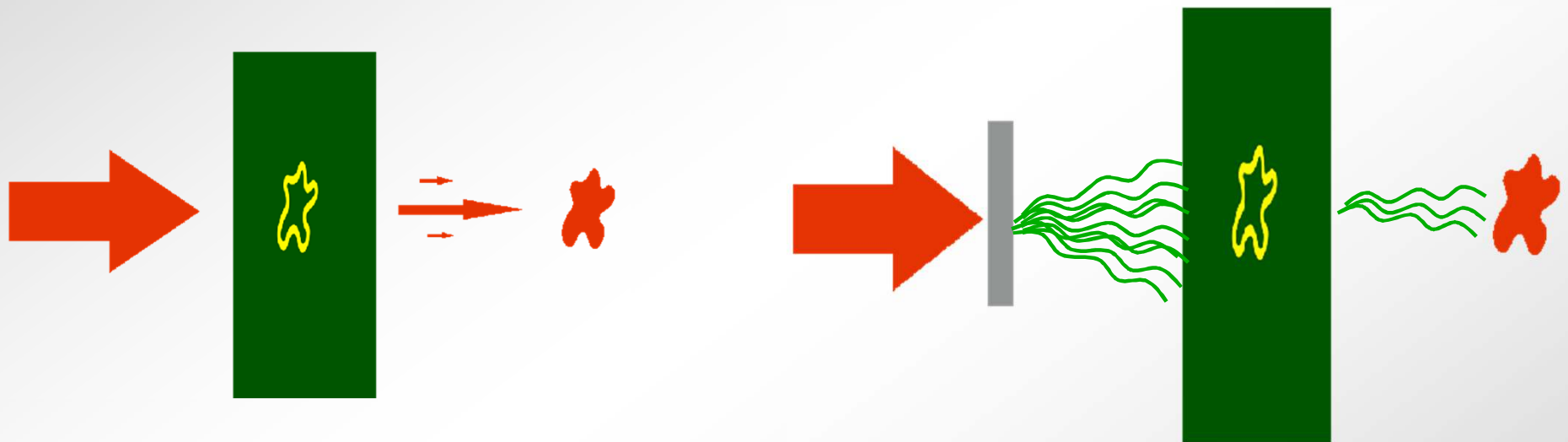
30 60 0 60 30

Resolution length on the detector (nm)

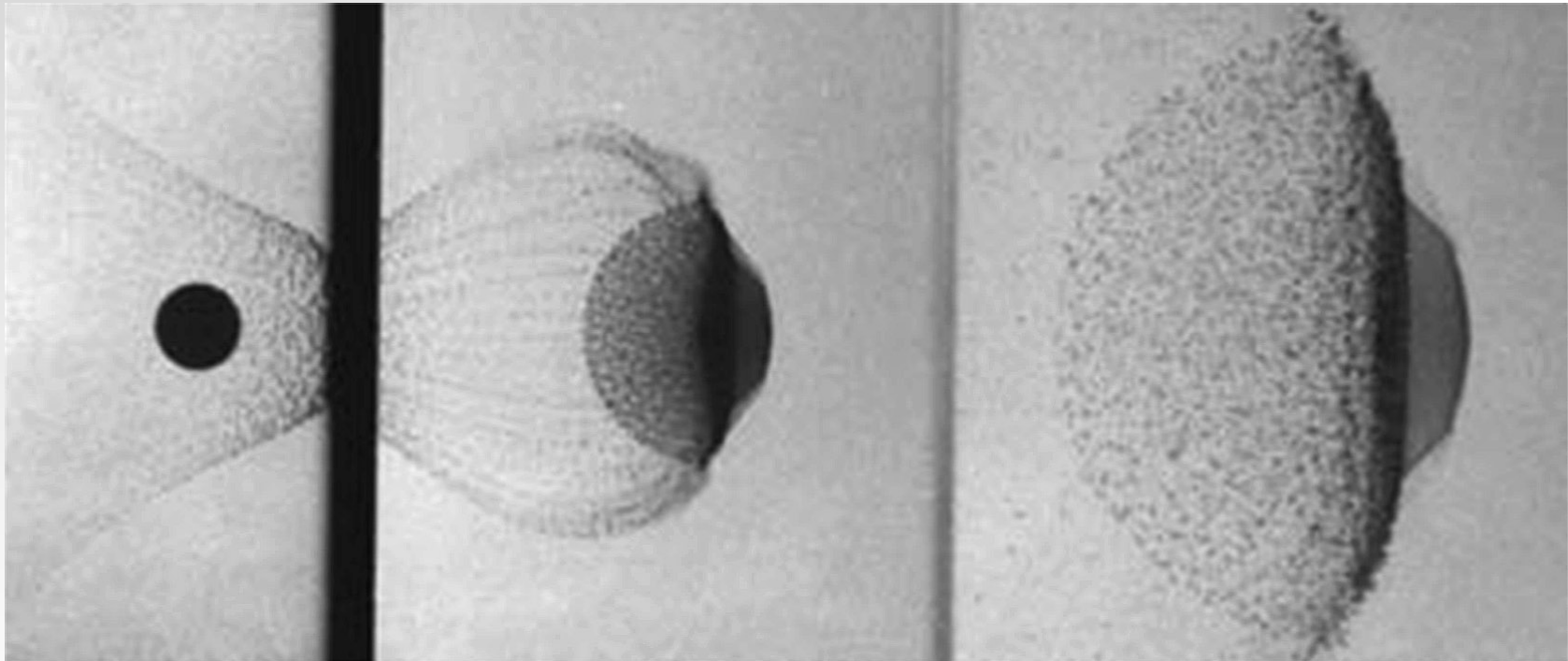
Thanks

J.Hajdu and H. Chapman

## Radiography



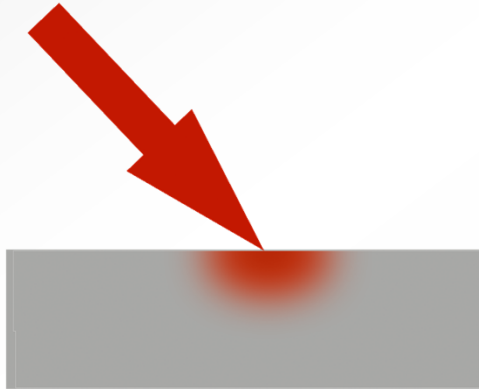
FOM: Signal/noise  $\implies$  Dose at 1 m & resolution (x,t)



Debris cloud produced  
by an Al sphere impacting  
a thin AL shield at hypervelocity.

Source: <http://www.udri.udayton.edu/NR/exeres/9E82E5F2-AC29-4467-8F15-0E5A7FEA48F3.htm>

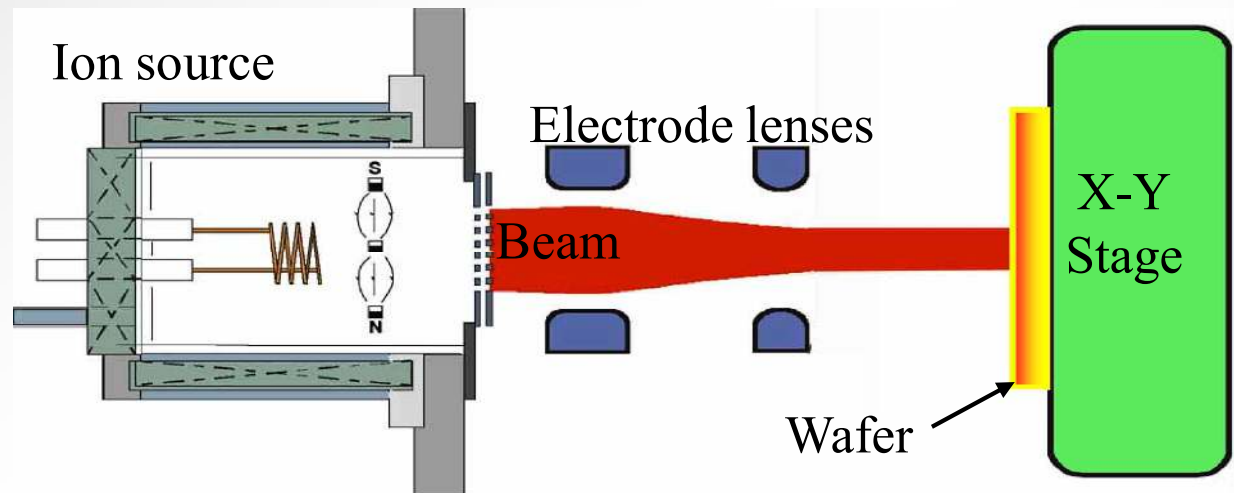
**Alter matter,  
induce chemistry**



FOM: process time  
process efficiency

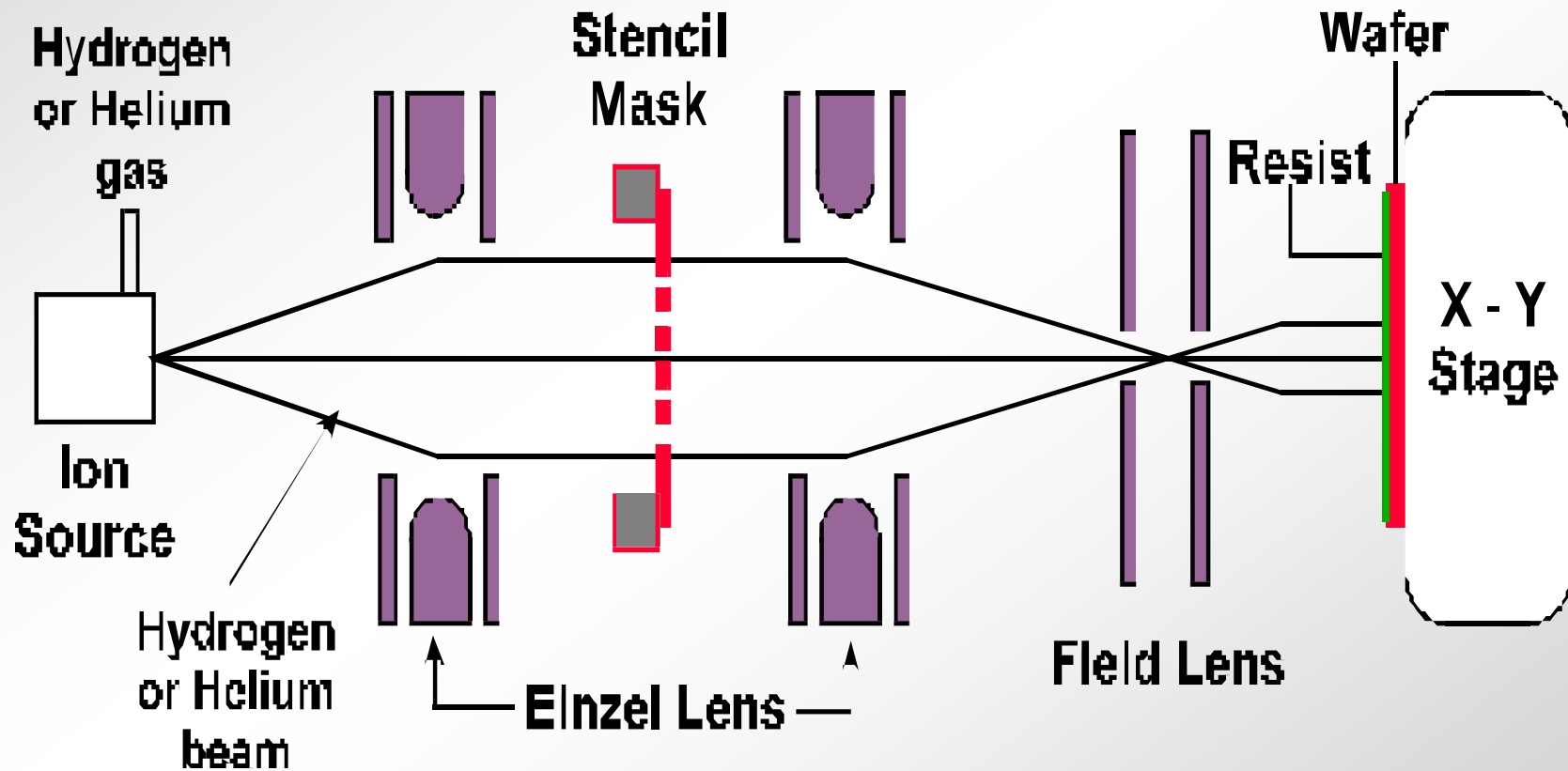


- ❖ Ions prepare Si wafers for further processing finally yielding integrated circuit chips
  - > 1 B\$/year business in semi-conductor “machine tools”



- ❖ Emerging areas
  - Flat-panel video displays
  - Ultra-high density electronics

a In conventional optical lithography the ion beam is replaced with a bright light source



a The Si wafer is coated with a photo-sensitive material (resist)

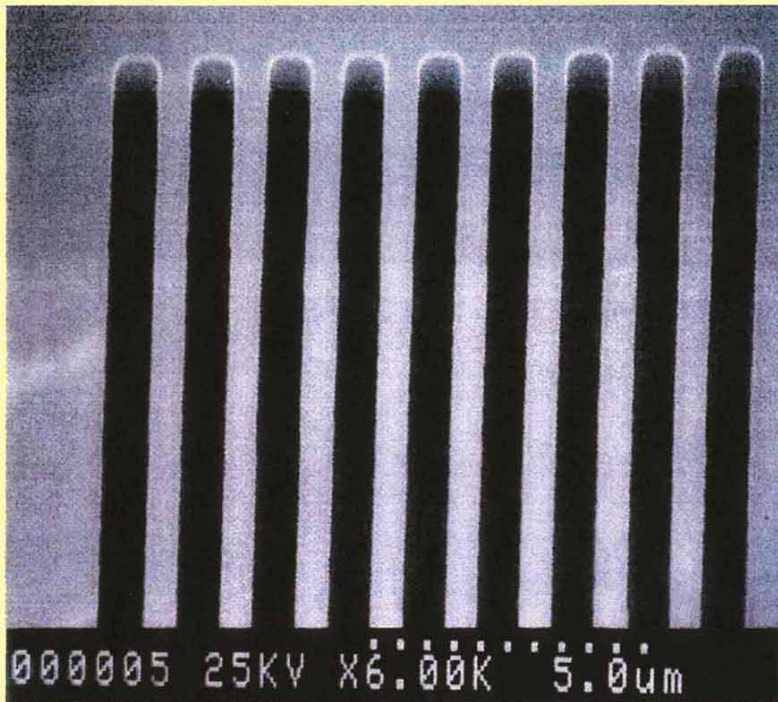


# Future industrial applications: Ion beam lithography

in 180 nm Shipley DUV resist UVI1HS

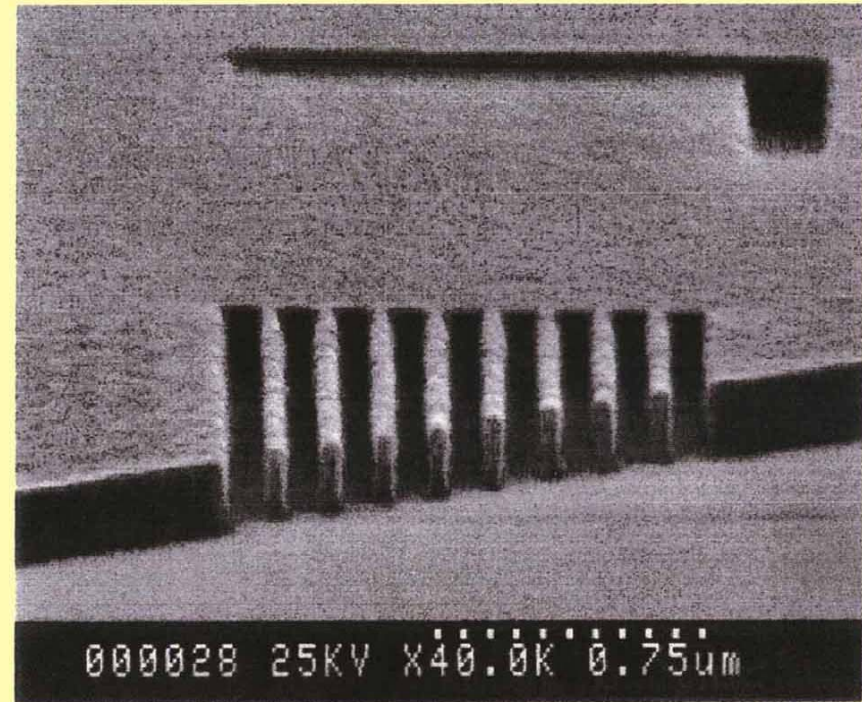
W. Bruenger  
FhG ISiT  
Nov 1999

Stencil Mask



Wafer

75 keV He<sup>+</sup> ions  
0.46  $\mu\text{C}/\text{cm}^2$   
exposure dose



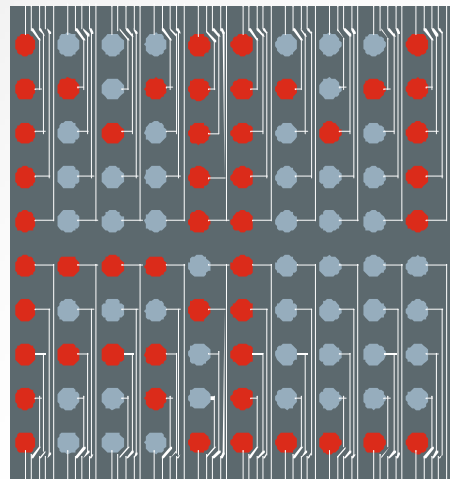
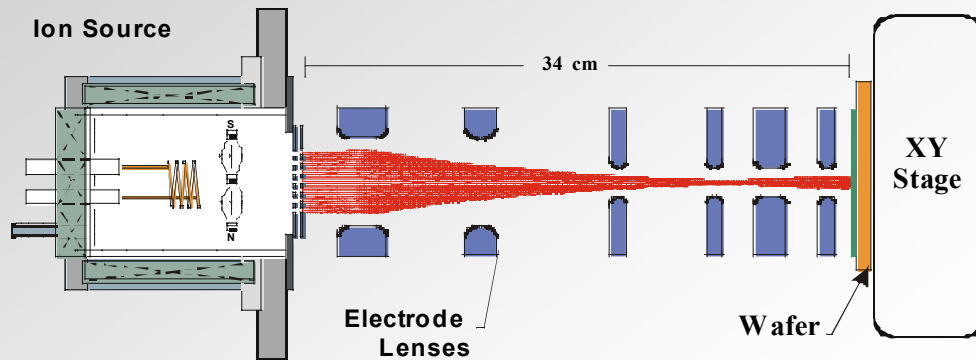
650 nm L/S

→ 8.7x reduction →

75 nm L/S



# Writing with a million beams: Maskless Micro-Beam Reduction Lithography

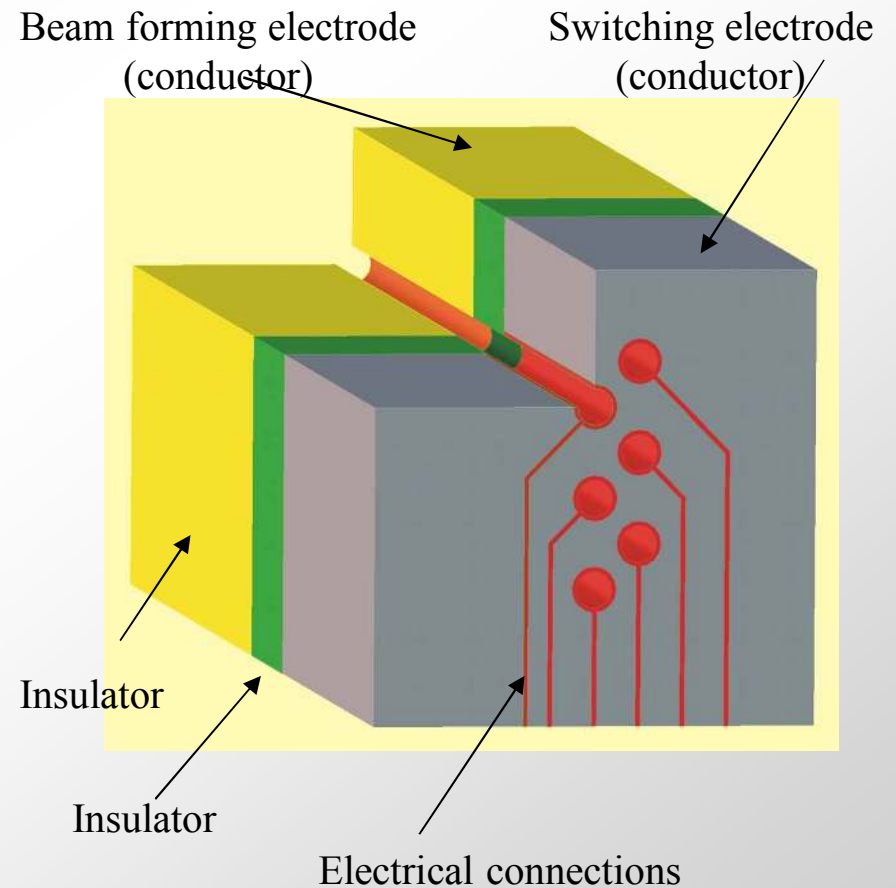


Direct projection



Projection  
and scanning

## Universal Pattern Generator Electrode Layout



## Therapy



FOM: treatment time  
tumor control probability  
precision beam control

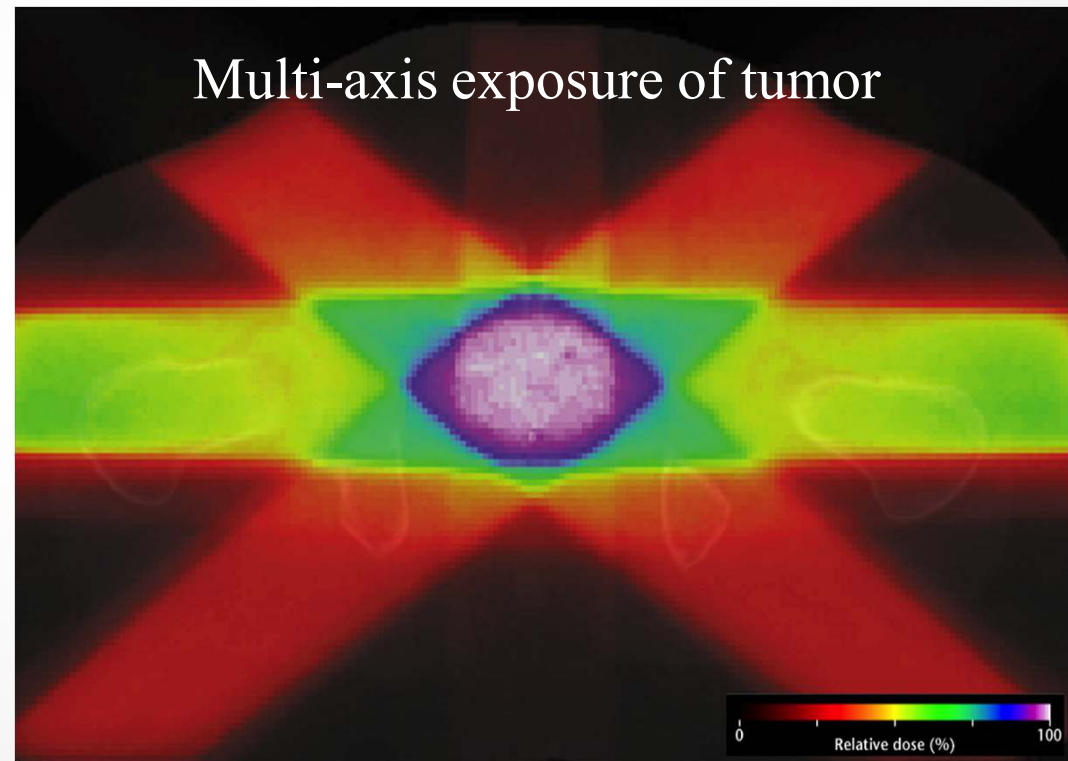




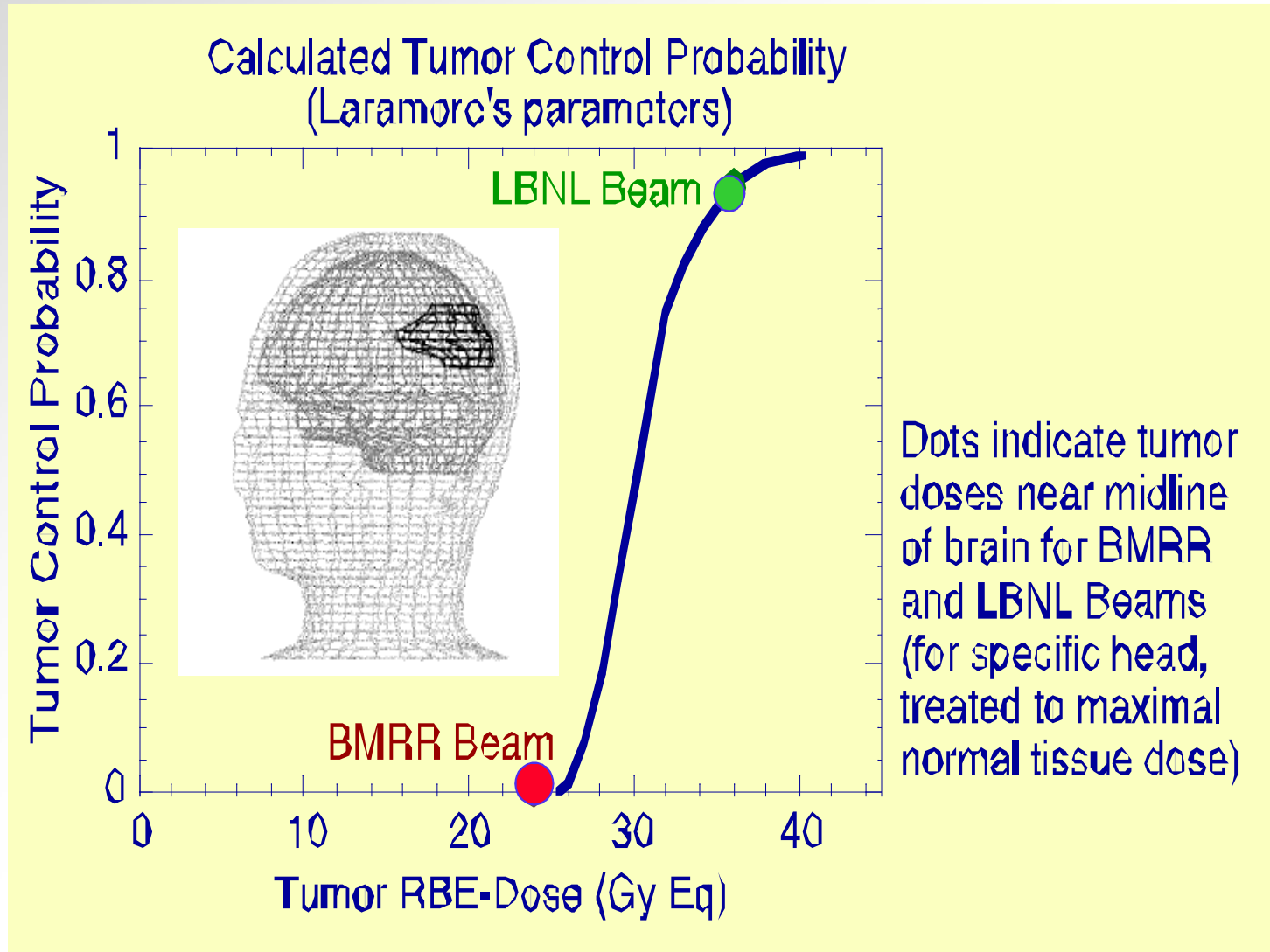
# Example: Conformal therapy



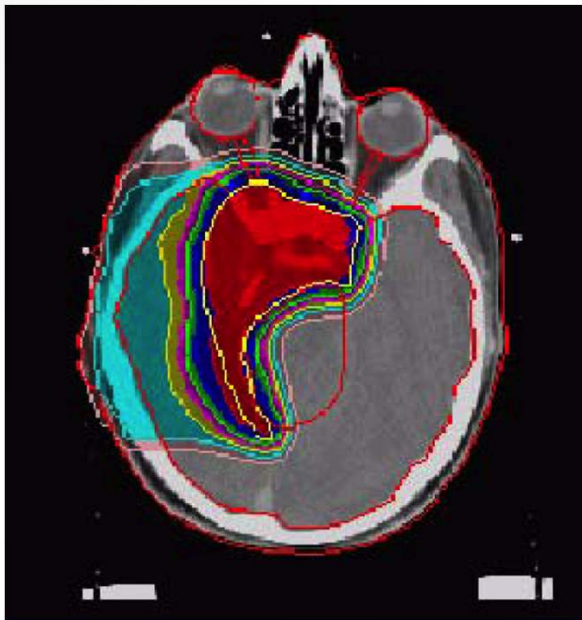
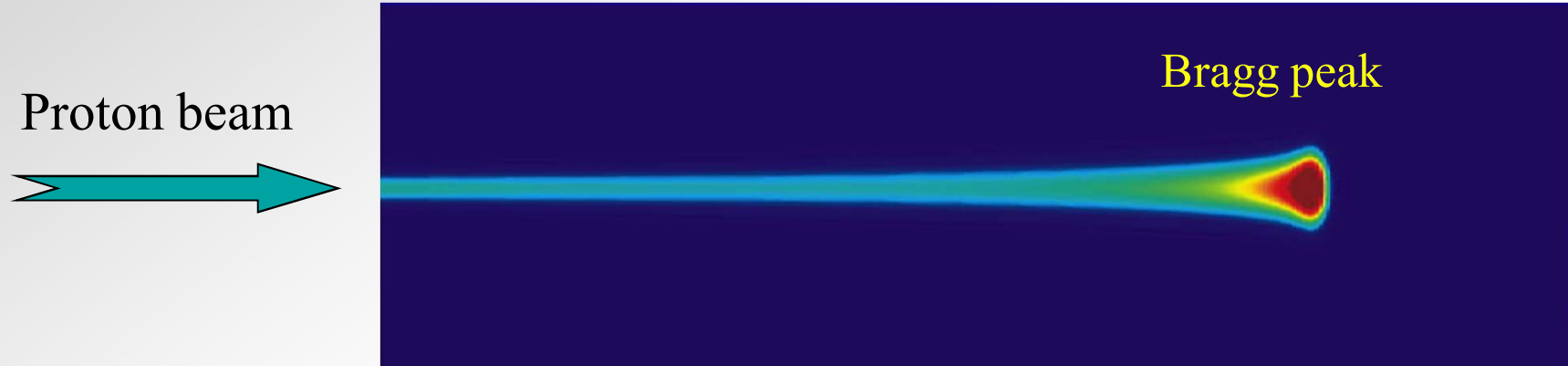
Challenge: Kill the tumor cells  
w/o killing healthy tissue



*Gamma rays from electron linac*



*Control of glioblastoma multiformae with neutron capture therapy*



*Hadron therapy allows for the best treatment of deep tumors with minimized dose to healthy tissue*



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

University of Ljubljana

FACULTY OF  
ECONOMICS

# Extracts from Comments from the Office of Science

**BESAC**

**27 February 2014**

Patricia M. Dehmer  
Acting Director, Office of Science

U.S. Department of Energy  
Office of Science

- Reflections on prioritization of science & scientific facilities
- Reflections on the impact of the BESAC Report on “Future X-Ray Light Sources”



# Scientific User Facilities of the Office of Science



## Support for Researchers

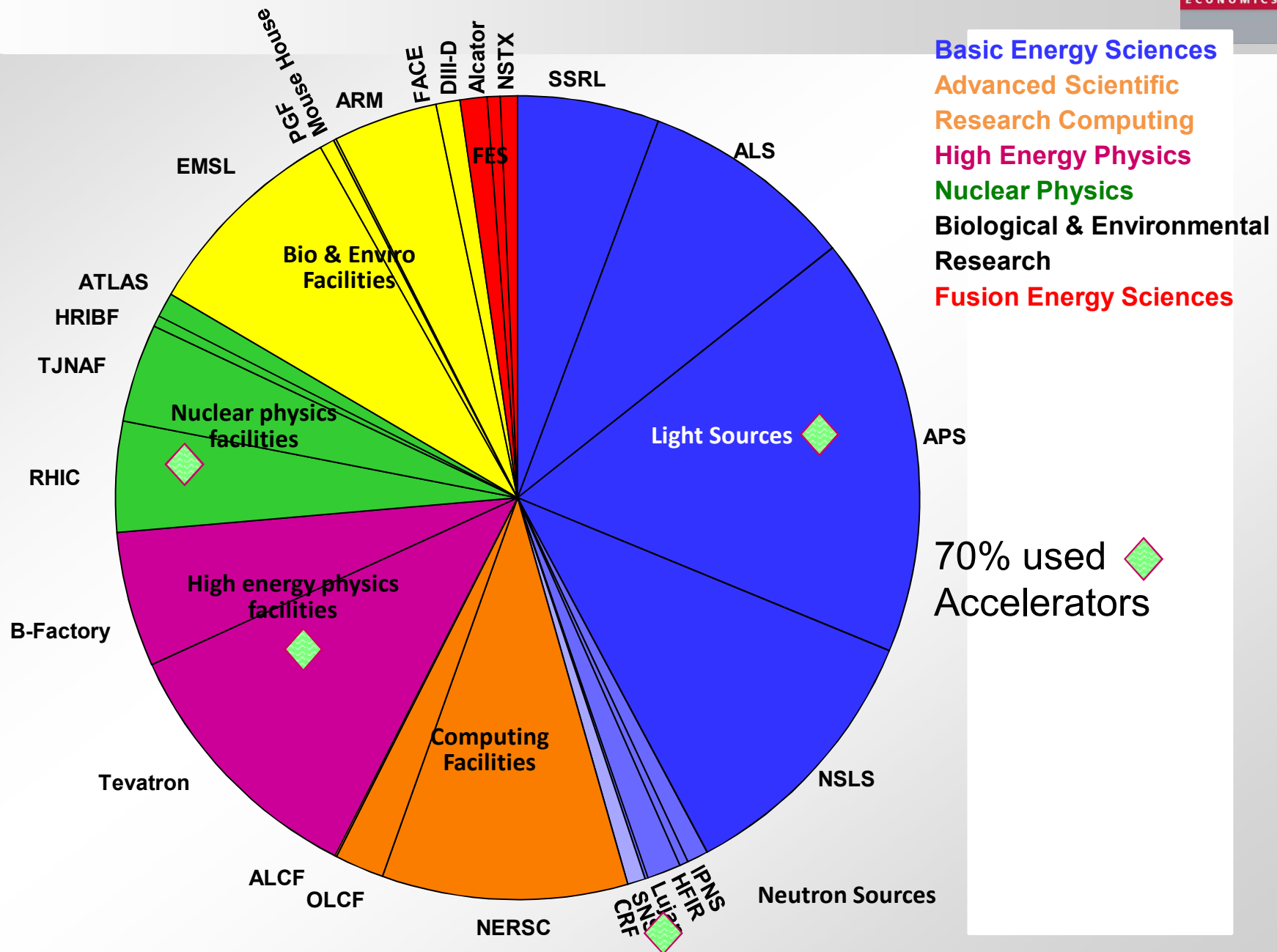
- ~**22,000** Ph.D. scientists, graduate students, undergraduates, engineers, & support staff at **>300** institutions.
- **47%** of Federal support of **basic research in the physical sciences** & key components of the Nation's basic research in biology and computing.
- Research that led to **> 100 Nobel Prizes** during the past **6** decades — **>20** in the past **10** years.

## Support for Scientific User Facilities

- World's largest collection of scientific user facilities to ~**28,000** users each year.



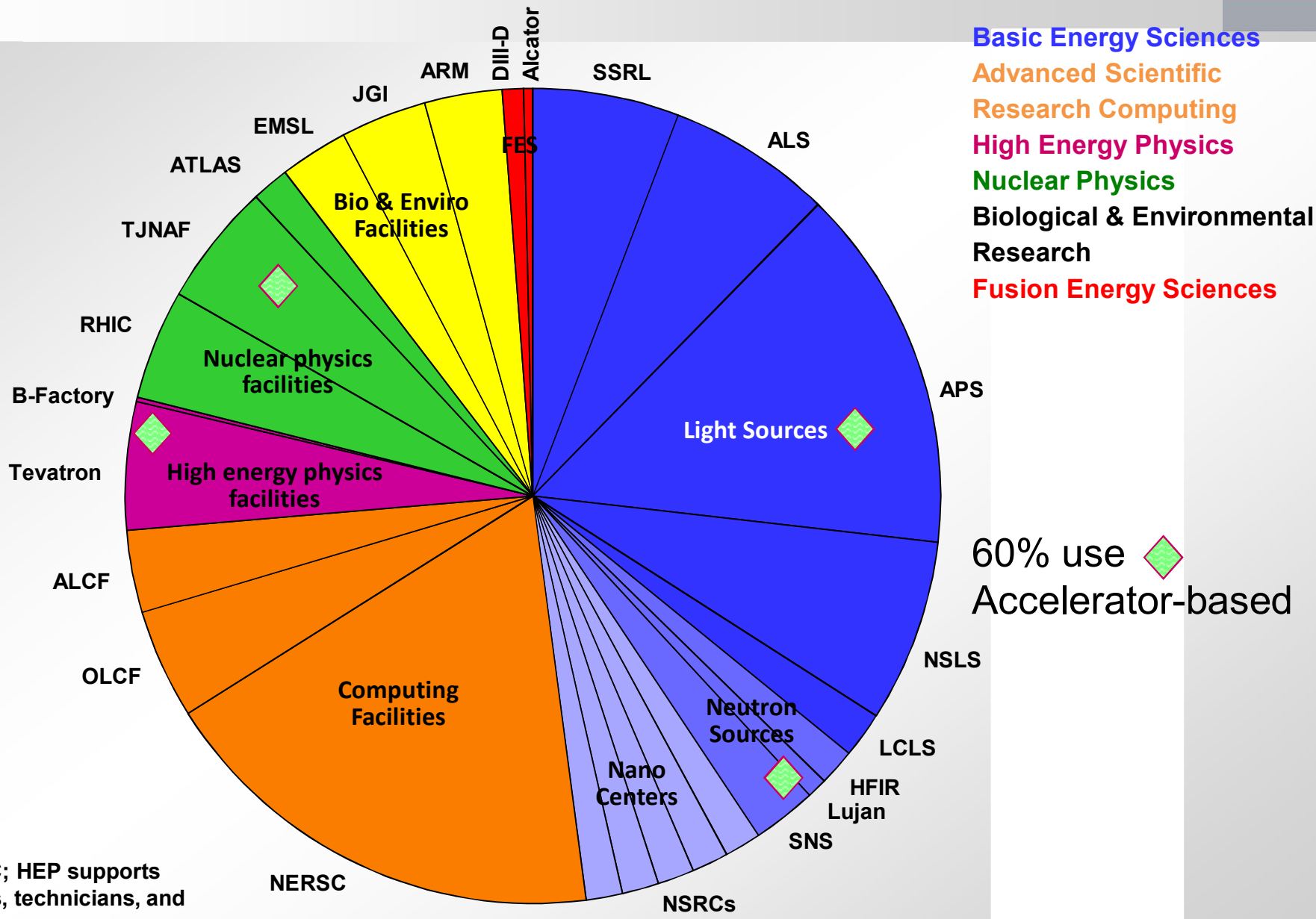
# Distribution of Users at the SC Facilities 2007



# Distribution of Users at the ~30 SC Facilities 2013

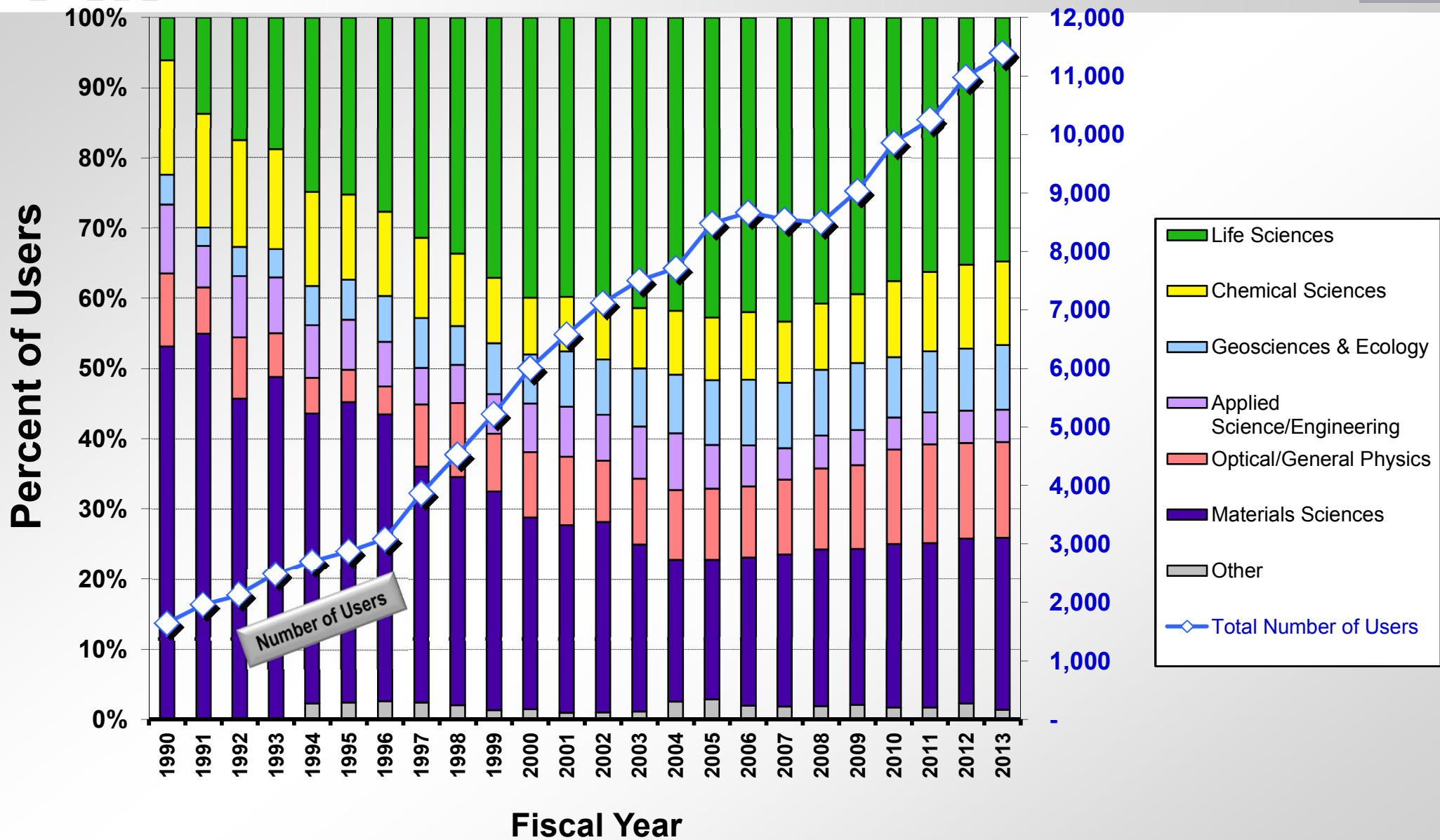


Nearly 3/4 of users do their work at ASCR or BES facilities



Does not include LHC; HEP supports about 1,700 scientists, technicians, and engineers at the LHC.

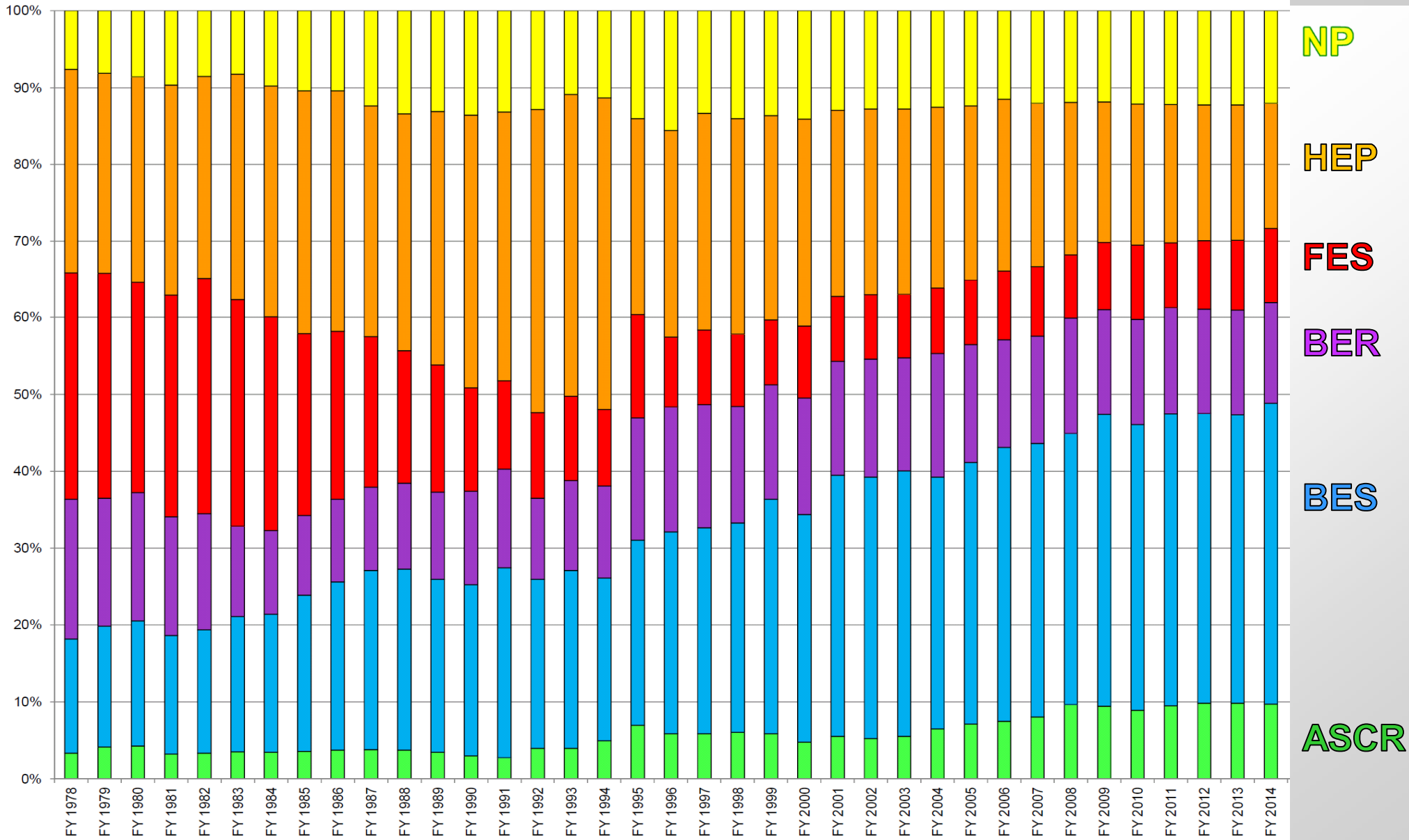
# Users by Discipline at the Light Sources







# Major SC Program Funding (% of total) FY 1978-2014



# A Summary of Terminated and New Major Facilities 1990-2015

- Basic Energy Sciences
- Advanced Scientific Research Computing
- High Energy Physics
- Nuclear Physics
- Biological & Environmental Research
- Fusion Energy Sciences

